# The Parma Polyhedra Library C Language Interface User's Manual\* (version 0.11.2)

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# 1 Main Page

All the declarations needed for using the PPL's C interface (preprocessor symbols, data types, variables and functions) are collected in the header file ppl\_c.h. This file, which is designed to work with pre-ANSI and ANSI C compilers as well as C99 and C++ compilers, should be included, either directly or via some other header file, with the directive

#include <ppl\_c.h>

If this directive does not work, then your compiler is unable to find the file ppl\_c.h. So check that the library is installed (if it is not installed, you may want to make install, perhaps with root privileges) in the right place (if not you may want to reconfigure the library using the appropriate pathname for the --prefix option); and that your compiler knows where it is installed (if not you should add the path to the directory where ppl\_c.h is located to the compiler's include file search path; this is usually done with the -I option).

The name space of the PPL's C interface is PPL\_\* for preprocessor symbols, enumeration values and variables; and ppl\_\* for data types and function names. The interface systematically uses *opaque data types* (generic pointers that completely hide the internal representations from the client code) and provides all required access functions. By using just the interface, the client code can exploit all the functionalities of the library yet avoid directly manipulating the library's data structures. The advantages are that (1)

applications do not depend on the internals of the library (these may change from release to release), and (2) the interface invariants can be thoroughly checked (by the access functions).

#### Note

All functions taking as input argument an opaque pointer datatype assume that such an argument is actually *referring to a valid PPL object*. For instance, a function with an argument having type ppl\_-MIP\_Problem\_t will expect a valid MIP\_Problem object, previously initialized by calling, e.g., ppl\_new\_MIP\_Problem. If that is not the case (e.g., if a null pointer is passed in), the behavior is undefined.

The PPL's C interface is initialized by means of the ppl\_initialize function. This function must be called *before using any other interface of the library*. The application can release the resources allocated by the library by calling the ppl\_finalize function. After this function is called *no other interface of the library may be used* until the interface is re-initialized using ppl\_initialize.

Any application using the PPL should make sure that only the intended version(s) of the library are ever used. The version used can be checked at compile-time thanks to the macros PPL\_VERSION\_MAJOR, PPL\_VERSION\_MINOR, PPL\_VERSION\_REVISION and PPL\_VERSION\_BETA, which give, respectively major, minor, revision and beta numbers of the PPL version. This is an example of their use:

```
#if PPL_VERSION_MAJOR == 0 && PPL_VERSION_MINOR < 6
# error "PPL version 0.6 or following is required"
#endif</pre>
```

Compile-time checking, however, is not normally enough, particularly in an environment where there is dynamic linking. Run-time checking can be performed by means of the functions ppl\_version\_major, ppl\_version\_minor, ppl\_version\_revision, and ppl\_version\_beta. The PPL's C interface also provides functions ppl\_version, returning character string containing the full version number, and ppl\_banner, returning a string that, in addition, provides (pointers to) other useful information for the library user.

All programs using the PPL's C interface must link with the following libraries: libppl\_c (PPL's C interface), libppl (PPL's core), libgmpxx (GMP's C++ interface), and libgmp (GMP's library core). On most Unix-like systems, this is done by adding -lppl\_c, -lppl, -lgmpxx, and -lgmp to the compiler's or linker's command line. For example:

gcc myprogram.o -lppl\_c -lppl -lgmpxx -lgmp

If this does not work, it means that your compiler/linker is not finding the libraries where it expects. Again, this could be because you forgot to install the library or you installed it in a non-standard location. In the latter case you will need to use the appropriate options (usually -L) and, if you use shared libraries, some sort of run-time path selection mechanisms. Consult your compiler's documentation for details. Notice that the PPL is built using Libtool and an application can exploit this fact to significantly simplify the linking phase. See Libtool's documentation for details. Those working under Linux can find a lot of useful information on how to use program libraries (including static, shared, and dynamically loaded libraries) in the Program Library HOWTO.

For examples on how to use the functions provided by the C interface, you are referred to the directory demos/ppl\_lpsol/ in the source distribution. It contains a *Mixed Integer (Linear) Programming* solver written in C. In order to use this solver you will need to install GLPK (the GNU Linear Programming Kit): this is used to read linear programs in MPS format.

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# 4 Module Index

### 4.1 Modules

Here is a list of all modules:

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Handling	23
Library Datatypes	24

The Parma Polyhedra Library C Language Interface User's Manual (version 0.11.2). See http://www.cs.unipr.it/ppl/ for more information.

# 5 Class Index

# 5.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

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### **6** Module Documentation

### 6.1 C Language Interface

The Parma Polyhedra Library comes equipped with an interface for the C language.

### 6.2 Library Initialization and Finalization

### Functions

- int ppl\_initialize (void) Initializes the Parma Polyhedra Library. This function must be called before any other function.
- int ppl\_finalize (void) Finalizes the Parma Polyhedra Library. This function must be called after any other function.
- int ppl\_set\_rounding\_for\_PPL (void) Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly.
- int ppl\_restore\_pre\_PPL\_rounding (void) Sets the FPU rounding mode as it was before initialization of the PPL.
- int ppl\_irrational\_precision (unsigned \*p)
   Writes to p the precision parameter used for irrational calculations.
- int ppl\_set\_irrational\_precision (unsigned p) Sets the precision parameter used for irrational calculations.

### 6.2.1 Detailed Description

Functions for initialization/finalization of the library, as well as setting/resetting of floating-point rounding mode.

### 6.2.2 Function Documentation

#### 6.2.2.1 int ppl\_initialize (void)

Initializes the Parma Polyhedra Library. This function must be called before any other function.

#### Returns

PPL\_ERROR\_INVALID\_ARGUMENT if the library was already initialized.

### 6.2.2.2 int ppl\_finalize (void)

Finalizes the Parma Polyhedra Library. This function must be called after any other function.

#### Returns

PPL\_ERROR\_INVALID\_ARGUMENT if the library was already finalized.

### 6.2.2.3 int ppl\_set\_rounding\_for\_PPL (void)

Sets the FPU rounding mode so that the PPL abstractions based on floating point numbers work correctly.

This is performed automatically at initialization-time. Calling this function is needed only if restore\_pre\_-PPL\_rounding() has been previously called.

#### 6.2.2.4 int ppl\_restore\_pre\_PPL\_rounding (void)

Sets the FPU rounding mode as it was before initialization of the PPL.

After calling this function it is absolutely necessary to call set\_rounding\_for\_PPL() before using any PPL abstractions based on floating point numbers. This is performed automatically at finalization-time.

### 6.2.2.5 int ppl\_set\_irrational\_precision (unsigned *p*)

Sets the precision parameter used for irrational calculations.

If p is less than or equal to INT\_MAX, sets the precision parameter used for irrational calculations to p. Then, in the irrational calculations returning an unbounded rational, (e.g., when computing a square root), the lesser between numerator and denominator will be limited to 2\*\*p.

### 6.3 Version Checking

### Defines

- #define PPL\_VERSION "0.11.2"
  - A string containing the PPL version.
- #define PPL\_VERSION\_MAJOR 0 The major number of the PPL version.
- #define PPL\_VERSION\_MINOR 11

The minor number of the PPL version.

• #define PPL\_VERSION\_REVISION 2

The revision number of the PPL version.

• #define PPL\_VERSION\_BETA 0

The beta number of the PPL version. This is zero for official releases and nonzero for development snapshots.

#### **Functions**

- int ppl\_version\_major (void) Returns the major number of the PPL version.
- int ppl\_version\_minor (void) Returns the minor number of the PPL version.
- int ppl\_version\_revision (void) Returns the revision number of the PPL version.
- int ppl\_version\_beta (void) Returns the beta number of the PPL version.
- int ppl\_version (const char \*\*p)
   Writes to \*p a pointer to a character string containing the PPL version.
- int ppl\_banner (const char \*\*p)

*Writes to \*p a pointer to a character string containing the PPL banner.* 

### 6.3.1 Detailed Description

Symbolic constants and functions related to library version checking.

### 6.3.2 Define Documentation

### 6.3.2.1 #define PPL\_VERSION "0.11.2"

A string containing the PPL version.

Let M and m denote the numbers associated to PPL\_VERSION\_MAJOR and PPL\_VERSION\_MINOR, respectively. The format of PPL\_VERSION is M "." m if both PPL\_VERSION\_REVISION (r) and PPL\_VERSION\_BETA (b)are zero, M "." m "pre" b if PPL\_VERSION\_REVISION is zero and PPL\_VERSION\_BETA is not zero, M "." m "." r if PPL\_VERSION\_REVISION is not zero and PPL\_VERSION\_BETA is zero, M "." m "." r "pre" b if neither PPL\_VERSION\_REVISION nor PPL\_VERSION\_BETA are zero.

### 6.3.3 Function Documentation

### 6.3.3.1 int ppl\_banner (const char \*\* *p*)

Writes to \*p a pointer to a character string containing the PPL banner.

The banner provides information about the PPL version, the licensing, the lack of any warranty whatsoever, the C++ compiler used to build the library, where to report bugs and where to look for further information.

### 6.4 Error Handling

### Enumerations

• enum ppl\_enum\_error\_code {

PPL\_ERROR\_OUT\_OF\_MEMORY, PPL\_ERROR\_INVALID\_ARGUMENT, PPL\_ERROR\_DOMAIN\_ERROR, PPL\_ERROR\_LENGTH\_ERROR,

PPL\_ARITHMETIC\_OVERFLOW, PPL\_STDIO\_ERROR, PPL\_ERROR\_INTERNAL\_ERROR, PPL\_ERROR\_UNKNOWN\_STANDARD\_EXCEPTION,

PPL\_ERROR\_UNEXPECTED\_ERROR, PPL\_TIMEOUT\_EXCEPTION, PPL\_ERROR\_LOGIC\_ERROR }

Defines the error codes that any function may return.

### Functions

• int ppl\_set\_error\_handler (void(\*h)(enum ppl\_enum\_error\_code code, const char \*description)) Installs the user-defined error handler pointed at by h.

#### 6.4.1 Detailed Description

Symbolic constants and functions related to error reporting/handling.

#### 6.4.2 Enumeration Type Documentation

### 6.4.2.1 enum ppl\_enum\_error\_code

Defines the error codes that any function may return.

#### **Enumerator:**

*PPL\_ERROR\_OUT\_OF\_MEMORY* The virtual memory available to the process has been exhausted.

**PPL\_ERROR\_INVALID\_ARGUMENT** A function has been invoked with an invalid argument. **PPL\_ERROR\_DOMAIN\_ERROR** A function has been invoked outside its domain of definition.

- *PPL\_ERROR\_LENGTH\_ERROR* The construction of an object that would exceed its maximum permitted size was attempted.
- **PPL\_ARITHMETIC\_OVERFLOW** An arithmetic overflow occurred and the computation was consequently interrupted. This can *only* happen in library's incarnations using bounded integers as coefficients.
- **PPL\_STDIO\_ERROR** An error occurred during a C input/output operation. A more precise indication of what went wrong is available via errno.
- **PPL\_ERROR\_INTERNAL\_ERROR** An internal error that was diagnosed by the PPL itself. This indicates a bug in the PPL.
- *PPL\_ERROR\_UNKNOWN\_STANDARD\_EXCEPTION* A standard exception has been raised by the C++ run-time environment. This indicates a bug in the PPL.
- **PPL\_ERROR\_UNEXPECTED\_ERROR** A totally unknown, totally unexpected error happened. This indicates a bug in the PPL.
- **PPL\_TIMEOUT\_EXCEPTION** An exception has been raised by the PPL as a timeout previously set by the user has expired.
- **PPL\_ERROR\_LOGIC\_ERROR** The client program attempted to use the PPL in a way that violates its internal logic. This happens, for instance, when the client attempts to use the timeout facilities on a system that does not support them.

#### 6.4.3 Function Documentation

6.4.3.1 int ppl\_set\_error\_handler (void(\*)(enum ppl\_enum\_error\_code code, const char \*description) h)

Installs the user-defined error handler pointed at by h.

The error handler takes an error code and a textual description that gives further information about the actual error. The C string containing the textual description is read-only and its existence is not guaranteed after the handler has returned.

### 6.5 Handling

### Functions

• int ppl\_set\_timeout (unsigned time)

Sets the timeout for computations whose completion could require an exponential amount of time.

• int ppl\_reset\_timeout (void)

Resets the timeout time so that the computation is not interrupted.

• int ppl\_set\_deterministic\_timeout (unsigned weight)

Sets a threshold for computations whose completion could require an exponential amount of time.

int ppl\_reset\_deterministic\_timeout (void)

Resets the deterministic timeout so that the computation is not interrupted.

### 6.5.1 Detailed Description

Functions for setting and resetting timeouts.

### 6.5.2 Function Documentation

### 6.5.2.1 int ppl\_set\_timeout (unsigned *time*)

Sets the timeout for computations whose completion could require an exponential amount of time.

#### Parameters

time The number of hundreths of seconds. It must be strictly greater than zero.

Computations taking exponential time will be interrupted some time after time hundreths of seconds have elapsed since the call to the timeout setting function. If the computation is interrupted that way, the interrupted function will return error code PPL\_TIMEOUT\_EXCEPTION. Otherwise, if the computation completes without being interrupted, then the timeout should be reset by calling ppl\_reset\_timeout().

#### 6.5.2.2 int ppl\_set\_deterministic\_timeout (unsigned weight)

Sets a threshold for computations whose completion could require an exponential amount of time.

#### **Parameters**

weight The maximum computational weight allowed. It must be strictly greater than zero.

Computations taking exponential time will be interrupted some time after reaching the weight complexity threshold. If the computation is interrupted that way, the interrupted function will return error code PPL\_-TIMEOUT\_EXCEPTION. Otherwise, if the computation completes without being interrupted, then the deterministic timeout should be reset by calling ppl\_reset\_deterministic\_timeout().

#### Note

This "timeout" checking functionality is said to be *deterministic* because it is not based on actual elapsed time. Its behavior will only depend on (some of the) computations performed in the PPL library and it will be otherwise independent from the computation environment (CPU, operating system, compiler, etc.).

### Warning

The weight mechanism is under alpha testing. In particular, there is still no clear relation between the weight threshold and the actual computational complexity. As a consequence, client applications should be ready to reconsider the tuning of these weight thresholds when upgrading to newer version of the PPL.

### 6.6 Library Datatypes

Typedefs for the library datatypes and related symbolic constants.

### Typedefs

- typedef size\_t ppl\_dimension\_type An unsigned integral type for representing space dimensions.
- typedef const char \* ppl\_io\_variable\_output\_function\_type (ppl\_dimension\_type var) *The type of output functions used for printing variables.*
- typedef struct ppl\_Coefficient\_tag \* ppl\_Coefficient\_t
   Opaque pointer.
- typedef struct ppl\_Coefficient\_tag const \* ppl\_const\_Coefficient\_t
   Opaque pointer to const object.
- typedef struct ppl\_Linear\_Expression\_tag \* ppl\_Linear\_Expression\_t
   Opaque pointer.
- typedef struct ppl\_Linear\_Expression\_tag const \* ppl\_const\_Linear\_Expression\_t Opaque pointer to const object.
- typedef struct ppl\_Constraint\_tag \* ppl\_Constraint\_t
   Opaque pointer.
- typedef struct ppl\_Constraint\_tag const \* ppl\_const\_Constraint\_t
   Opaque pointer to const object.
- typedef struct ppl\_Constraint\_System\_tag \* ppl\_Constraint\_System\_t Opaque pointer.
- typedef struct ppl\_Constraint\_System\_tag const \* ppl\_const\_Constraint\_System\_t Opaque pointer to const object.
- typedef struct ppl\_Constraint\_System\_const\_iterator\_tag \* ppl\_Constraint\_System\_const\_iterator\_t

Opaque pointer.

 typedef struct ppl\_Constraint\_System\_const\_iterator\_tag const \* ppl\_const\_Constraint\_System\_const\_iterator\_t

Opaque pointer to const object.

- typedef struct ppl\_Generator\_tag \* ppl\_Generator\_t Opaque pointer.
- typedef struct ppl\_Generator\_tag const \* ppl\_const\_Generator\_t Opaque pointer to const object.
- typedef struct ppl\_Generator\_System\_tag \* ppl\_Generator\_System\_t
   Opaque pointer.
- typedef struct ppl\_Generator\_System\_tag const \* ppl\_const\_Generator\_System\_t

Opaque pointer to const object.

- typedef struct ppl\_Generator\_System\_const\_iterator\_tag \* ppl\_Generator\_System\_const\_iterator\_t Opaque pointer.
- typedef struct ppl\_Generator\_System\_const\_iterator\_tag const \* ppl\_const\_Generator\_System\_const\_iterator\_t

Opaque pointer to const object.

- typedef struct ppl\_Congruence\_tag \* ppl\_Congruence\_t
   Opaque pointer.
- typedef struct ppl\_Congruence\_tag const \* ppl\_const\_Congruence\_t Opaque pointer to const object.
- typedef struct ppl\_Congruence\_System\_tag \* ppl\_Congruence\_System\_t Opaque pointer.
- typedef struct ppl\_Congruence\_System\_tag const \* ppl\_const\_Congruence\_System\_t Opaque pointer to const object.
- typedef struct ppl\_Congruence\_System\_const\_iterator\_tag \* ppl\_Congruence\_System\_const\_iterator\_t

Opaque pointer.

 typedef struct ppl\_Congruence\_System\_const\_iterator\_tag const \* ppl\_const\_Congruence\_-System\_const\_iterator\_t

Opaque pointer to const object.

- typedef struct ppl\_Grid\_Generator\_tag \* ppl\_Grid\_Generator\_t Opaque pointer.
- typedef struct ppl\_Grid\_Generator\_tag const \* ppl\_const\_Grid\_Generator\_t Opaque pointer to const object.
- typedef struct ppl\_Grid\_Generator\_System\_tag \* ppl\_Grid\_Generator\_System\_t Opaque pointer.
- typedef struct ppl\_Grid\_Generator\_System\_tag const \* ppl\_const\_Grid\_Generator\_System\_t Opaque pointer to const object.
- typedef struct ppl\_Grid\_Generator\_System\_const\_iterator\_tag \* ppl\_Grid\_Generator\_System\_const\_iterator\_t

Opaque pointer.

 typedef struct ppl\_Grid\_Generator\_System\_const\_iterator\_tag const \* ppl\_const\_Grid\_Generator\_-System\_const\_iterator\_t

Opaque pointer to const object.

• typedef struct ppl\_MIP\_Problem\_tag \* ppl\_MIP\_Problem\_t

Opaque pointer.

- typedef struct ppl\_MIP\_Problem\_tag const \* ppl\_const\_MIP\_Problem\_t
   Opaque pointer to const object.
- typedef struct ppl\_PIP\_Problem\_tag \* ppl\_PIP\_Problem\_t
   Opaque pointer.
- typedef struct ppl\_PIP\_Problem\_tag const \* ppl\_const\_PIP\_Problem\_t
   Opaque pointer to const object.
- typedef struct ppl\_PIP\_Tree\_Node\_tag \* ppl\_PIP\_Tree\_Node\_t Opaque pointer.
- typedef struct ppl\_PIP\_Tree\_Node\_tag const \* ppl\_const\_PIP\_Tree\_Node\_t
   Opaque pointer to const object.
- typedef struct ppl\_PIP\_Decision\_Node\_tag \* ppl\_PIP\_Decision\_Node\_t
   Opaque pointer.
- typedef struct ppl\_PIP\_Decision\_Node\_tag const \* ppl\_const\_PIP\_Decision\_Node\_t
   Opaque pointer to const object.
- typedef struct ppl\_PIP\_Solution\_Node\_tag \* ppl\_PIP\_Solution\_Node\_t Opaque pointer.
- typedef struct ppl\_PIP\_Solution\_Node\_tag const \* ppl\_const\_PIP\_Solution\_Node\_t Opaque pointer to const object.
- typedef struct ppl\_Artificial\_Parameter\_tag \* ppl\_Artificial\_Parameter\_t
   Opaque pointer.
- typedef struct ppl\_Artificial\_Parameter\_tag const \* ppl\_const\_Artificial\_Parameter\_t Opaque pointer to const object.
- typedef struct ppl\_Artificial\_Parameter\_Sequence\_tag \* ppl\_Artificial\_Parameter\_Sequence\_t Opaque pointer.
- typedef struct ppl\_Artificial\_Parameter\_Sequence\_tag const \* ppl\_const\_Artificial\_Parameter\_-Sequence\_t

Opaque pointer to const object.

 typedef struct ppl\_Artificial\_Parameter\_Sequence\_const\_iterator\_tag \* ppl\_Artificial\_Parameter\_-Sequence\_const\_iterator\_t

Opaque pointer.

• typedef struct ppl\_Artificial\_Parameter\_Sequence\_const\_iterator\_tag const \* ppl\_const\_Artificial\_-Parameter\_Sequence\_const\_iterator\_t

Opaque pointer to const object.

- typedef struct ppl\_Polyhedron\_tag \* ppl\_Polyhedron\_t
   Opaque pointer.
- typedef struct ppl\_Polyhedron\_tag const \* ppl\_const\_Polyhedron\_t
   Opaque pointer to const object.
- typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag \* ppl\_Pointset\_Powerset\_C\_Polyhedron\_t

Opaque pointer.

 typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag const \* ppl\_const\_Pointset\_Powerset\_C\_-Polyhedron\_t

Opaque pointer to const object.

 typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_tag \* ppl\_Pointset\_Powerset\_C\_-Polyhedron\_iterator\_t

*Opaque pointer.* 

 typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_tag const \* ppl\_const\_Pointset\_-Powerset\_C\_Polyhedron\_iterator\_t

Opaque pointer to const object.

• typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_tag \* ppl\_Pointset\_Powerset\_-C\_Polyhedron\_const\_iterator\_t

Opaque pointer.

 typedef struct ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_tag const \* ppl\_const\_-Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t

Opaque pointer to const object.

#### Enumerations

• enum ppl\_enum\_Constraint\_Type {

PPL\_CONSTRAINT\_TYPE\_LESS\_THAN, PPL\_CONSTRAINT\_TYPE\_LESS\_OR\_EQUAL, PPL\_CONSTRAINT\_TYPE\_EQUAL, PPL\_CONSTRAINT\_TYPE\_GREATER\_OR\_EQUAL,

### PPL\_CONSTRAINT\_TYPE\_GREATER\_THAN }

Describes the relations represented by a constraint.

enum ppl\_enum\_Generator\_Type { PPL\_GENERATOR\_TYPE\_LINE, PPL\_GENERATOR\_TYPE\_RAY, PPL\_GENERATOR\_TYPE\_POINT, PPL\_GENERATOR\_TYPE\_CLOSURE\_POINT }

Describes the different kinds of generators.

• enum ppl\_enum\_Grid\_Generator\_Type { PPL\_GRID\_GENERATOR\_TYPE\_LINE, PPL\_GRID\_ GENERATOR\_TYPE\_PARAMETER, PPL\_GRID\_GENERATOR\_TYPE\_POINT }

Describes the different kinds of grid generators.

- enum ppl\_enum\_Bounded\_Integer\_Type\_Width {
   PPL\_BITS\_8, PPL\_BITS\_16, PPL\_BITS\_32, PPL\_BITS\_64,
   PPL\_BITS\_128 }
   Widths of bounded integer types.
- enum ppl\_enum\_Bounded\_Integer\_Type\_Representation { PPL\_UNSIGNED, PPL\_SIGNED\_2\_-COMPLEMENT }

Representation of bounded integer types.

- enum ppl\_enum\_Bounded\_Integer\_Type\_Overflow { PPL\_OVERFLOW\_WRAPS, PPL\_-OVERFLOW\_UNDEFINED, PPL\_OVERFLOW\_IMPOSSIBLE }
  - Overflow behavior of bounded integer types.

### Functions

- int ppl\_max\_space\_dimension (ppl\_dimension\_type \*m)
   Writes to m the maximum space dimension this library can handle.
- int ppl\_not\_a\_dimension (ppl\_dimension\_type \*m) Writes to m a value that does not designate a valid dimension.
- int ppl\_io\_print\_variable (ppl\_dimension\_type var) Pretty-prints var to stdout.
- int ppl\_io\_fprint\_variable (FILE \*stream, ppl\_dimension\_type var) Pretty-prints var to the given output stream.
- int ppl\_io\_asprint\_variable (char \*\*strp, ppl\_dimension\_type var)
   Pretty-prints var to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_io\_set\_variable\_output\_function (ppl\_io\_variable\_output\_function\_type \*p) Sets the output function to be used for printing variables to p.
- int ppl\_io\_get\_variable\_output\_function (ppl\_io\_variable\_output\_function\_type \*\*pp) Writes a pointer to the current variable output function to pp.
- char \* ppl\_io\_wrap\_string (const char \*src, unsigned indent\_depth, unsigned preferred\_first\_line\_length, unsigned preferred\_line\_length)
   Utility function for the wrapping of lines of text.

#### Variables

- unsigned int PPL\_COMPLEXITY\_CLASS\_POLYNOMIAL Code of the worst-case polynomial complexity class.
- unsigned int PPL\_COMPLEXITY\_CLASS\_SIMPLEX Code of the worst-case exponential but typically polynomial complexity class.

- unsigned int PPL\_COMPLEXITY\_CLASS\_ANY Code of the universal complexity class.
- unsigned int PPL\_POLY\_CON\_RELATION\_IS\_DISJOINT Individual bit saying that the polyhedron and the set of points satisfying the constraint are disjoint.
- unsigned int PPL\_POLY\_CON\_RELATION\_STRICTLY\_INTERSECTS Individual bit saying that the polyhedron intersects the set of points satisfying the constraint, but it is not included in it.
- unsigned int PPL\_POLY\_CON\_RELATION\_IS\_INCLUDED Individual bit saying that the polyhedron is included in the set of points satisfying the constraint.
- unsigned int PPL\_POLY\_CON\_RELATION\_SATURATES Individual bit saying that the polyhedron is included in the set of points saturating the constraint.
- unsigned int PPL\_POLY\_GEN\_RELATION\_SUBSUMES Individual bit saying that adding the generator would not change the polyhedron.

#### 6.6.1 Detailed Description

Typedefs for the library datatypes and related symbolic constants. The datatypes provided by the library should be manipulated by means of the corresponding opaque pointer types and the functions working on them.

#### Note

To simplify the detection of common programming mistakes, we provide both pointer-to-const and pointer-to-nonconst opaque pointers, with implicit conversions mapping each pointer-to-nonconst to the corresponding pointer-to-const when needed. The user of the C interface is therefore recommended to adopt the pointer-to-const type whenever read-only access is meant.

#### 6.6.2 Typedef Documentation

#### 6.6.2.1 typedef const char\* ppl\_io\_variable\_output\_function\_type(ppl\_dimension\_type var)

The type of output functions used for printing variables.

An output function for variables must write a textual representation for var to a character buffer, nullterminate it, and return a pointer to the beginning of the buffer. In case the operation fails, 0 should be returned and perhaps errno should be set in a meaningful way. The library does nothing with the buffer, besides printing its contents.

#### 6.6.3 Enumeration Type Documentation

#### 6.6.3.1 enum ppl\_enum\_Constraint\_Type

Describes the relations represented by a constraint.

### **Enumerator:**

**PPL\_CONSTRAINT\_TYPE\_LESS\_THAN** The constraint is of the form e < 0. **PPL\_CONSTRAINT\_TYPE\_LESS\_OR\_EQUAL** The constraint is of the form  $e \le 0$ . **PPL\_CONSTRAINT\_TYPE\_EQUAL** The constraint is of the form e = 0. **PPL\_CONSTRAINT\_TYPE\_GREATER\_OR\_EQUAL** The constraint is of the form  $e \ge 0$ . **PPL\_CONSTRAINT\_TYPE\_GREATER\_THAN** The constraint is of the form e > 0.

6.6.3.2 enum ppl\_enum\_Generator\_Type

Describes the different kinds of generators.

### **Enumerator:**

PPL\_GENERATOR\_TYPE\_LINE The generator is a line.
PPL\_GENERATOR\_TYPE\_RAY The generator is a ray.
PPL\_GENERATOR\_TYPE\_POINT The generator is a point.
PPL\_GENERATOR\_TYPE\_CLOSURE\_POINT The generator is a closure point.

### 6.6.3.3 enum ppl\_enum\_Grid\_Generator\_Type

Describes the different kinds of grid generators.

### **Enumerator:**

PPL\_GRID\_GENERATOR\_TYPE\_LINE The grid generator is a line.PPL\_GRID\_GENERATOR\_TYPE\_PARAMETER The grid generator is a parameter.PPL\_GRID\_GENERATOR\_TYPE\_POINT The grid generator is a point.

### 6.6.3.4 enum ppl\_enum\_Bounded\_Integer\_Type\_Width

Widths of bounded integer types.

#### **Enumerator:**

PPL\_BITS\_8 8 bits.
PPL\_BITS\_16 16 bits.
PPL\_BITS\_32 32 bits.
PPL\_BITS\_64 64 bits.
PPL\_BITS\_128 128 bits.

### 6.6.3.5 enum ppl\_enum\_Bounded\_Integer\_Type\_Representation

Representation of bounded integer types.

### **Enumerator:**

**PPL\_UNSIGNED** Unsigned binary.

*PPL\_SIGNED\_2\_COMPLEMENT* Signed binary where negative values are represented by the two's complement of the absolute value.

### 6.6.3.6 enum ppl\_enum\_Bounded\_Integer\_Type\_Overflow

Overflow behavior of bounded integer types.

### **Enumerator:**

- **PPL\_OVERFLOW\_WRAPS** On overflow, wrapping takes place. This means that, for a w-bit bounded integer, the computation happens modulo  $2^w$ .
- **PPL\_OVERFLOW\_UNDEFINED** On overflow, the result is undefined. This simply means that the result of the operation resulting in an overflow can take any value.

### Note

Even though something more serious can happen in the system being analyzed ---due to, e.g., C's undefined behavior---, here we are only concerned with the results of arithmetic operations. It is the responsibility of the analyzer to ensure that other manifestations of undefined behavior are conservatively approximated.

**PPL\_OVERFLOW\_IMPOSSIBLE** Overflow is impossible. This is for the analysis of languages where overflow is trapped before it affects the state, for which, thus, any indication that an overflow may have affected the state is necessarily due to the imprecision of the analysis.

### 6.6.4 Function Documentation

6.6.4.1 char\* ppl\_io\_wrap\_string (const char \* src, unsigned indent\_depth, unsigned preferred\_first\_line\_length, unsigned preferred\_line\_length)

Utility function for the wrapping of lines of text.

### Parameters

src The source string holding the text to wrap.

*indent\_depth* The indentation depth.

preferred\_first\_line\_length The preferred length for the first line of text.

*preferred\_line\_length* The preferred length for all the lines but the first one.

### Returns

The wrapped string in a malloc-allocated buffer.

# 7 Class Documentation

### 7.1 ppl\_Artificial\_Parameter\_Sequence\_const\_iterator\_tag Interface Reference

Types and functions for iterating on PIP artificial parameters.

#include <ppl\_c\_header.h>

### **Related Functions**

(Note that these are not member functions.)

#### **Constructors, Assignment and Destructor**

• int ppl\_new\_Artificial\_Parameter\_Sequence\_const\_iterator (ppl\_Artificial\_Parameter\_-Sequence\_const\_iterator\_t \*papit)

Builds a new 'const iterator' and writes a handle to it at address papit.

• int ppl\_new\_Artificial\_Parameter\_Sequence\_const\_iterator\_from\_Artificial\_Parameter\_-Sequence\_const\_iterator (ppl\_Artificial\_Parameter\_Sequence\_const\_iterator\_t \*papit, ppl\_const\_Artificial\_Parameter\_Sequence\_const\_iterator\_t apit)

Builds a const iterator that is a copy of apit; writes a handle for the newly created const iterator at address papit.

• int ppl\_assign\_Artificial\_Parameter\_Sequence\_const\_iterator\_from\_Artificial\_Parameter\_-Sequence\_const\_iterator (ppl\_Artificial\_Parameter\_Sequence\_const\_iterator\_t dst, ppl\_const\_-Artificial\_Parameter\_Sequence\_const\_iterator\_t src)

Assigns a copy of the const iterator src to dst.

• int ppl\_delete\_Artificial\_Parameter\_Sequence\_const\_iterator (ppl\_const\_Artificial\_Parameter\_-Sequence\_const\_iterator\_t apit)

Invalidates the handle apit: this makes sure the corresponding resources will eventually be released.

### Dereferencing, Incrementing and Equality Testing

• int ppl\_Artificial\_Parameter\_Sequence\_const\_iterator\_dereference (ppl\_const\_Artificial\_-Parameter\_Sequence\_const\_iterator\_t apit, ppl\_const\_Artificial\_Parameter\_t \*pap)

Dereference apit writing a const handle to the resulting artificial parameter at address pap.

• int ppl\_Artificial\_Parameter\_Sequence\_const\_iterator\_increment (ppl\_Artificial\_Parameter\_-Sequence\_const\_iterator\_t apit)

Increment apit so that it "points" to the next artificial parameter.

• int ppl\_Artificial\_Parameter\_Sequence\_const\_iterator\_equal\_test (ppl\_const\_Artificial\_-Parameter\_Sequence\_const\_iterator\_t x, ppl\_const\_Artificial\_Parameter\_Sequence\_const\_iterator\_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

### 7.1.1 Detailed Description

Types and functions for iterating on PIP artificial parameters.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

### 7.2 ppl\_Artificial\_Parameter\_tag Interface Reference

Types and functions for PIP artificial parameters.

```
#include <ppl_c_header.h>
```

#### **Related Functions**

(Note that these are not member functions.)

• int ppl\_Artificial\_Parameter\_get\_Linear\_Expression (ppl\_const\_Artificial\_Parameter\_t ap, ppl\_-Linear\_Expression\_t le)

Copies into le the linear expression in artificial parameter ap.

• int ppl\_Artificial\_Parameter\_coefficient (ppl\_const\_Artificial\_Parameter\_t ap, ppl\_dimension\_type var, ppl\_Coefficient\_t n)

Copies into n the coefficient of variable var in the artificial parameter ap.

• int ppl\_Artificial\_Parameter\_get\_inhomogeneous\_term (ppl\_const\_Artificial\_Parameter\_t ap, ppl\_Coefficient\_t n)

Copies into n the inhomogeneous term of the artificial parameter ap.

int ppl\_Artificial\_Parameter\_denominator (ppl\_const\_Artificial\_Parameter\_t ap, ppl\_Coefficient\_t n)

Copies into n the denominator in artificial parameter ap.

#### **Input/Output Functions**

- int ppl\_io\_print\_Artificial\_Parameter (ppl\_const\_Artificial\_Parameter\_t x) *Prints x to stdout.*
- int ppl\_io\_fprint\_Artificial\_Parameter (FILE \*stream, ppl\_const\_Artificial\_Parameter\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_Artificial\_Parameter (char \*\*strp, ppl\_const\_Artificial\_Parameter\_t x) Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Artificial\_Parameter\_ascii\_dump (ppl\_const\_Artificial\_Parameter\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_Artificial\_Parameter\_ascii\_load (ppl\_Artificial\_Parameter\_t x, FILE \*stream) Loads an ascii representation of x from stream.

## 7.2.1 Detailed Description

Types and functions for PIP artificial parameters. The types and functions for PIP artificial parameters provide an interface towards *Artificial\_Parameter*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.3 ppl\_Coefficient\_tag Interface Reference

Types and functions for coefficients.

#include <ppl\_c\_header.h>

# **Related Functions**

(Note that these are not member functions.)

#### **Constructors, Assignment and Destructor**

- int ppl\_new\_Coefficient (ppl\_Coefficient\_t \*pc)
   Creates a new coefficient with value 0 and writes a handle for the newly created coefficient at address pc.
- int ppl\_new\_Coefficient\_from\_mpz\_t (ppl\_Coefficient\_t \*pc, mpz\_t z)
   Creates a new coefficient with the value given by the GMP integer z and writes a handle for the newly created coefficient at address pc.
- int ppl\_new\_Coefficient\_from\_Coefficient (ppl\_Coefficient\_t \*pc, ppl\_const\_Coefficient\_t c) Builds a coefficient that is a copy of c; writes a handle for the newly created coefficient at address pc.
- int ppl\_assign\_Coefficient\_from\_mpz\_t (ppl\_Coefficient\_t dst, mpz\_t z) Assign to dst the value given by the GMP integer z.
- int ppl\_assign\_Coefficient\_from\_Coefficient (ppl\_Coefficient\_t dst, ppl\_const\_Coefficient\_t src) Assigns a copy of the coefficient src to dst.
- int ppl\_delete\_Coefficient (ppl\_const\_Coefficient\_t c)
   Invalidates the handle c: this makes sure the corresponding resources will eventually be released.

## **Read-Only Accessor Functions**

- int ppl\_Coefficient\_to\_mpz\_t (ppl\_const\_Coefficient\_t c, mpz\_t z) Sets the value of the GMP integer z to the value of c.
- int ppl\_Coefficient\_OK (ppl\_const\_Coefficient\_t c)
   *Returns a positive integer if c is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if c is broken. Useful for debugging purposes.*
- int ppl\_Coefficient\_is\_bounded (void) *Returns a positive integer if coefficients are bounded; returns 0 otherwise.*

• int ppl\_Coefficient\_min (mpz\_t min)

Returns a positive integer if coefficients are bounded, in which case min is set to their minimum value; returns 0 otherwise.

• int ppl\_Coefficient\_max (mpz\_t max)

Returns a positive integer if coefficients are bounded, in which case max is set to their maximum value; returns 0 otherwise.

# **I/O Functions**

- int ppl\_io\_print\_Coefficient (ppl\_const\_Coefficient\_t x) Prints x to stdout.
- int ppl\_io\_fprint\_Coefficient (FILE \*stream, ppl\_const\_Coefficient\_t x)
   Prints x to the given output stream.
- int ppl\_io\_asprint\_Coefficient (char \*\*strp, ppl\_const\_Coefficient\_t x)
   Prints x to a malloc-allocated string, a pointer to which is returned via strp.

## 7.3.1 Detailed Description

Types and functions for coefficients. The types and functions for coefficients provide an interface towards *Coefficient*. Depending on configuration, the PPL coefficients may be implemented by the unbounded precision integers provided by GMP (default), or by bounded precision integers (with checks for overflows).

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.4 ppl\_Congruence\_System\_const\_iterator\_tag Interface Reference

Types and functions for iterating on congruence systems.

#include <ppl\_c\_header.h>

## **Related Functions**

(Note that these are not member functions.)

## **Constructors, Assignment and Destructor**

int ppl\_new\_Congruence\_System\_const\_iterator (ppl\_Congruence\_System\_const\_iterator\_t \*pcit)

Builds a new 'const iterator' and writes a handle to it at address pcit.

• int ppl\_new\_Congruence\_System\_const\_iterator\_from\_Congruence\_System\_const\_iterator (ppl\_Congruence\_System\_const\_iterator\_t \*pcit, ppl\_const\_Congruence\_System\_const\_iterator\_t cit)

Builds a const iterator that is a copy of cit; writes a handle for the newly created const iterator at address pcit.

• int ppl\_assign\_Congruence\_System\_const\_iterator\_from\_Congruence\_System\_const\_iterator (ppl\_Congruence\_System\_const\_iterator\_t dst, ppl\_const\_Congruence\_System\_const\_iterator\_t src)

Assigns a copy of the const iterator src to dst.

• int ppl\_delete\_Congruence\_System\_const\_iterator (ppl\_const\_Congruence\_System\_const\_iterator\_t cit)

Invalidates the handle cit: this makes sure the corresponding resources will eventually be released.

## **Dereferencing, Incrementing and Equality Testing**

 int ppl\_Congruence\_System\_const\_iterator\_dereference (ppl\_const\_Congruence\_System\_const\_iterator\_t cit, ppl\_const\_Congruence\_t \*pc)

Dereference cit writing a const handle to the resulting congruence at address pc.

• int ppl\_Congruence\_System\_const\_iterator\_increment (ppl\_Congruence\_System\_const\_iterator\_t cit)

Increment cit so that it "points" to the next congruence.

• int ppl\_Congruence\_System\_const\_iterator\_equal\_test (ppl\_const\_Congruence\_System\_const\_iterator\_t x, ppl\_const\_Congruence\_System\_const\_iterator\_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

# 7.4.1 Detailed Description

Types and functions for iterating on congruence systems. The types and functions for congruence systems iterators provide read-only access to the elements of a congruence system by interfacing *Congruence\_System::const\_iterator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.5 ppl\_Congruence\_System\_tag Interface Reference

Types and functions for congruence systems.

```
#include <ppl_c_header.h>
```

# **Related Functions**

(Note that these are not member functions.)

## **Constructors, Assignment and Destructor**

int ppl\_new\_Congruence\_System (ppl\_Congruence\_System\_t \*pcs)
 Builds an empty system of congruences and writes a handle to it at address pcs.

- int ppl\_new\_Congruence\_System\_zero\_dim\_empty (ppl\_Congruence\_System\_t \*pcs) Builds a zero-dimensional, unsatisfiable congruence system and writes a handle to it at address pcs.
- int ppl\_new\_Congruence\_System\_from\_Congruence (ppl\_Congruence\_System\_t \*pcs, ppl\_const\_Congruence\_t c)

Builds the singleton congruence system containing only a copy of congruence c; writes a handle for the newly created system at address pcs.

• int ppl\_new\_Congruence\_System\_from\_Congruence\_System (ppl\_Congruence\_System\_t \*pcs, ppl\_const\_Congruence\_System\_t cs)

Builds a congruence system that is a copy of cs; writes a handle for the newly created system at address pcs.

• int ppl\_assign\_Congruence\_System\_from\_Congruence\_System (ppl\_Congruence\_System\_t dst, ppl\_const\_Congruence\_System\_t src)

Assigns a copy of the congruence system src to dst.

• int ppl\_delete\_Congruence\_System (ppl\_const\_Congruence\_System\_t cs) Invalidates the handle cs: this makes sure the corresponding resources will eventually be released.

## Functions that Do Not Modify the Congruence System

 int ppl\_Congruence\_System\_space\_dimension (ppl\_const\_Congruence\_System\_t cs, ppl\_dimension\_type \*m)

Writes to m the dimension of the vector space enclosing cs.

- int ppl\_Congruence\_System\_empty (ppl\_const\_Congruence\_System\_t cs) Returns a positive integer if cs contains no (non-trivial) congruence; returns 0 otherwise.
- int ppl\_Congruence\_System\_begin (ppl\_const\_Congruence\_System\_t cs, ppl\_Congruence\_System\_const\_iterator\_t cit)

Assigns to cit a const iterator "pointing" to the beginning of the congruence system cs.

• int ppl\_Congruence\_System\_end (ppl\_const\_Congruence\_System\_t cs, ppl\_Congruence\_System\_const\_iterator\_t cit)

Assigns to cit a const iterator "pointing" past the end of the congruence system cs.

• int ppl\_Congruence\_System\_OK (ppl\_const\_Congruence\_System\_t cs)

Returns a positive integer if cs is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if cs is broken. Useful for debugging purposes.

## Functions that May Modify the Congruence System

- int ppl\_Congruence\_System\_clear (ppl\_Congruence\_System\_t cs) *Removes all the congruences from the congruence system cs and sets its space dimension to 0.*
- int ppl\_Congruence\_System\_insert\_Congruence (ppl\_Congruence\_System\_t cs, ppl\_const\_-Congruence\_t c)

Inserts a copy of the congruence c into cs; the space dimension is increased, if necessary.

# **Input/Output Functions**

- int ppl\_io\_print\_Congruence\_System (ppl\_const\_Congruence\_System\_t x) Prints x to stdout.
- int ppl\_io\_fprint\_Congruence\_System (FILE \*stream, ppl\_const\_Congruence\_System\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_Congruence\_System (char \*\*strp, ppl\_const\_Congruence\_System\_t x) Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Congruence\_System\_ascii\_dump (ppl\_const\_Congruence\_System\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_Congruence\_System\_ascii\_load (ppl\_Congruence\_System\_t x, FILE \*stream) Loads an ascii representation of x from stream.

## 7.5.1 Detailed Description

Types and functions for congruence systems. The types and functions for congruence systems provide an interface towards *Congruence\_System*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.6 ppl\_Congruence\_tag Interface Reference

Types and functions for congruences.

#include <ppl\_c\_header.h>

# **Related Functions**

(Note that these are not member functions.)

#### **Constructors, Assignment and Destructor**

 int ppl\_new\_Congruence (ppl\_Congruence\_t \*pc, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_-Coefficient\_t m)

Creates the new congruence  $le = 0 \pmod{m}$  and writes a handle for it at address pc. The space dimension of the new congruence is equal to the space dimension of le.

• int ppl\_new\_Congruence\_zero\_dim\_false (ppl\_Congruence\_t \*pc)

*Creates the unsatisfiable (zero-dimension space) congruence*  $0 = 1 \pmod{0}$  *and writes a handle for it at address* pc.

- int ppl\_new\_Congruence\_zero\_dim\_integrality (ppl\_Congruence\_t \*pc)
   Creates the true (zero-dimension space) congruence 0 = 1 (mod 1), also known as integrality congruence. A handle for the newly created congruence is written at address pc.
- int ppl\_new\_Congruence\_from\_Congruence (ppl\_Congruence\_t \*pc, ppl\_const\_Congruence\_t c)

Builds a congruence that is a copy of c; writes a handle for the newly created congruence at address pc.

• int ppl\_assign\_Congruence\_from\_Congruence (ppl\_Congruence\_t dst, ppl\_const\_Congruence\_t src)

Assigns a copy of the congruence src to dst.

• int ppl\_delete\_Congruence (ppl\_const\_Congruence\_t c) Invalidates the handle c: this makes sure the corresponding resources will eventually be released.

## Functions that Do Not Modify the Congruence

- int ppl\_Congruence\_space\_dimension (ppl\_const\_Congruence\_t c, ppl\_dimension\_type \*m) Writes to m the space dimension of c.
- int ppl\_Congruence\_coefficient (ppl\_const\_Congruence\_t c, ppl\_dimension\_type var, ppl\_Coefficient\_t n)

Copies into n the coefficient of variable var in congruence c.

- int ppl\_Congruence\_inhomogeneous\_term (ppl\_const\_Congruence\_t c, ppl\_Coefficient\_t n) Copies into n the inhomogeneous term of congruence c.
- int ppl\_Congruence\_modulus (ppl\_const\_Congruence\_t c, ppl\_Coefficient\_t m) Copies into m the modulus of congruence c.
- int ppl\_Congruence\_OK (ppl\_const\_Congruence\_t c) *Returns a positive integer if c is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if c is broken. Useful for debugging purposes.*

#### **Input/Output Functions**

- int ppl\_io\_print\_Congruence (ppl\_const\_Congruence\_t x) Prints x to stdout.
- int ppl\_io\_fprint\_Congruence (FILE \*stream, ppl\_const\_Congruence\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_Congruence (char \*\*strp, ppl\_const\_Congruence\_t x) *Prints x to a malloc-allocated string, a pointer to which is returned via strp.*
- int ppl\_Congruence\_ascii\_dump (ppl\_const\_Congruence\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_Congruence\_ascii\_load (ppl\_Congruence\_t x, FILE \*stream) Loads an ascii representation of x from stream.

# 7.6.1 Detailed Description

Types and functions for congruences. The types and functions for congruences provide an interface towards *Congruence*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.7 ppl\_Constraint\_System\_const\_iterator\_tag Interface Reference

Types and functions for iterating on constraint systems.

#include <ppl\_c\_header.h>

## **Related Functions**

(Note that these are not member functions.)

#### **Constructors, Assignment and Destructor**

- int ppl\_new\_Constraint\_System\_const\_iterator (ppl\_Constraint\_System\_const\_iterator\_t \*pcit) Builds a new 'const iterator' and writes a handle to it at address pcit.
- int ppl\_new\_Constraint\_System\_const\_iterator\_from\_Constraint\_System\_const\_iterator (ppl\_Constraint\_System\_const\_iterator\_t \*pcit, ppl\_const\_Constraint\_System\_const\_iterator\_t cit) Builds a const iterator that is a copy of cit; writes a handle for the newly created const iterator at address pcit.
- int ppl\_assign\_Constraint\_System\_const\_iterator\_from\_Constraint\_System\_const\_iterator (ppl\_Constraint\_System\_const\_iterator\_t dst, ppl\_const\_Constraint\_System\_const\_iterator\_t src) Assigns a copy of the const iterator src to dst.
- int ppl\_delete\_Constraint\_System\_const\_iterator (ppl\_const\_Constraint\_System\_const\_iterator\_t cit)

Invalidates the handle cit: this makes sure the corresponding resources will eventually be released.

#### **Dereferencing, Incrementing and Equality Testing**

• int ppl\_Constraint\_System\_const\_iterator\_dereference (ppl\_const\_Constraint\_System\_const\_iterator\_t cit, ppl\_const\_Constraint\_t \*pc)

Dereference cit writing a const handle to the resulting constraint at address pc.

• int ppl\_Constraint\_System\_const\_iterator\_increment (ppl\_Constraint\_System\_const\_iterator\_t cit)

Increment cit so that it "points" to the next constraint.

• int ppl\_Constraint\_System\_const\_iterator\_equal\_test (ppl\_const\_Constraint\_System\_const\_iterator\_t x, ppl\_const\_Constraint\_System\_const\_iterator\_t y)

# 7.7.1 Detailed Description

Types and functions for iterating on constraint systems. The types and functions for constraint systems iterators provide read-only access to the elements of a constraint system by interfacing *Constraint\_-System::const\_iterator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

# 7.8 ppl\_Constraint\_System\_tag Interface Reference

Types and functions for constraint systems.

#include <ppl\_c\_header.h>

## **Related Functions**

(Note that these are not member functions.)

### **Constructors, Assignment and Destructor**

- int ppl\_new\_Constraint\_System (ppl\_Constraint\_System\_t \*pcs)
   Builds an empty system of constraints and writes a handle to it at address pcs.
- int ppl\_new\_Constraint\_System\_zero\_dim\_empty (ppl\_Constraint\_System\_t \*pcs) Builds a zero-dimensional, unsatisfiable constraint system and writes a handle to it at address pcs.
- int ppl\_new\_Constraint\_System\_from\_Constraint (ppl\_Constraint\_System\_t \*pcs, ppl\_const\_-Constraint\_t c)

Builds the singleton constraint system containing only a copy of constraint c; writes a handle for the newly created system at address pcs.

int ppl\_new\_Constraint\_System\_from\_Constraint\_System (ppl\_Constraint\_System\_t \*pcs, ppl\_const\_Constraint\_System\_t cs)

Builds a constraint system that is a copy of cs; writes a handle for the newly created system at address pcs.

• int ppl\_assign\_Constraint\_System\_from\_Constraint\_System (ppl\_Constraint\_System\_t dst, ppl\_const\_Constraint\_System\_t src)

Assigns a copy of the constraint system src to dst.

• int ppl\_delete\_Constraint\_System (ppl\_const\_Constraint\_System\_t cs) Invalidates the handle cs: this makes sure the corresponding resources will eventually be released.

## Functions that Do Not Modify the Constraint System

 int ppl\_Constraint\_System\_space\_dimension (ppl\_const\_Constraint\_System\_t cs, ppl\_dimension\_type \*m)

Writes to m the dimension of the vector space enclosing cs.

- int ppl\_Constraint\_System\_empty (ppl\_const\_Constraint\_System\_t cs) Returns a positive integer if cs contains no (non-trivial) constraint; returns 0 otherwise.
- int ppl\_Constraint\_System\_has\_strict\_inequalities (ppl\_const\_Constraint\_System\_t cs) Returns a positive integer if cs contains any (non-trivial) strict inequality; returns 0 otherwise.
- int ppl\_Constraint\_System\_begin (ppl\_const\_Constraint\_System\_t cs, ppl\_Constraint\_System\_const\_iterator\_t cit)

Assigns to cit a const iterator "pointing" to the beginning of the constraint system cs.

• int ppl\_Constraint\_System\_end (ppl\_const\_Constraint\_System\_t cs, ppl\_Constraint\_System\_const\_iterator\_t cit) Assigns to cit a const iterator "pointing" past the end of the constraint system cs.

• int ppl\_Constraint\_System\_OK (ppl\_const\_Constraint\_System\_t cs)

Returns a positive integer if cs is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if cs is broken. Useful for debugging purposes.

# Functions that May Modify the Constraint System

- int ppl\_Constraint\_System\_clear (ppl\_Constraint\_System\_t cs) Removes all the constraints from the constraint system cs and sets its space dimension to 0.
- int ppl\_Constraint\_System\_insert\_Constraint (ppl\_Constraint\_System\_t cs, ppl\_const\_Constraint\_t c)

Inserts a copy of the constraint c into cs; the space dimension is increased, if necessary.

## **Input/Output Functions**

- int ppl\_io\_print\_Constraint\_System (ppl\_const\_Constraint\_System\_t x)
   Prints x to stdout.
- int ppl\_io\_fprint\_Constraint\_System (FILE \*stream, ppl\_const\_Constraint\_System\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_Constraint\_System (char \*\*strp, ppl\_const\_Constraint\_System\_t x) Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Constraint\_System\_ascii\_dump (ppl\_const\_Constraint\_System\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_Constraint\_System\_ascii\_load (ppl\_Constraint\_System\_t x, FILE \*stream) Loads an ascii representation of x from stream.

# 7.8.1 Detailed Description

Types and functions for constraint systems. The types and functions for constraint systems provide an interface towards *Constraint\_System*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.9 ppl\_Constraint\_tag Interface Reference

Types and functions for constraints.

#include <ppl\_c\_header.h>

# **Related Functions**

(Note that these are not member functions.)

#### **Constructors, Assignment and Destructor**

• int ppl\_new\_Constraint (ppl\_Constraint\_t \*pc, ppl\_const\_Linear\_Expression\_t le, enum ppl\_enum\_Constraint\_Type rel)

Creates the new constraint 'le rel0' and writes a handle for it at address pc. The space dimension of the new constraint is equal to the space dimension of le.

- int ppl\_new\_Constraint\_zero\_dim\_false (ppl\_Constraint\_t \*pc)
   Creates the unsatisfiable (zero-dimension space) constraint 0 = 1 and writes a handle for it at address pc.
- int ppl\_new\_Constraint\_zero\_dim\_positivity (ppl\_Constraint\_t \*pc)
   Creates the true (zero-dimension space) constraint 0 ≤ 1, also known as positivity constraint. A handle for the newly created constraint is written at address pc.
- int ppl\_new\_Constraint\_from\_Constraint (ppl\_Constraint\_t \*pc, ppl\_const\_Constraint\_t c) Builds a constraint that is a copy of c; writes a handle for the newly created constraint at address pc.
- int ppl\_assign\_Constraint\_from\_Constraint (ppl\_Constraint\_t dst, ppl\_const\_Constraint\_t src) Assigns a copy of the constraint src to dst.
- int ppl\_delete\_Constraint (ppl\_const\_Constraint\_t c) Invalidates the handle c: this makes sure the corresponding resources will eventually be released.

## Functions that Do Not Modify the Constraint

- int ppl\_Constraint\_space\_dimension (ppl\_const\_Constraint\_t c, ppl\_dimension\_type \*m) Writes to m the space dimension of c.
- int ppl\_Constraint\_type (ppl\_const\_Constraint\_t c) *Returns the type of constraint c.*
- int ppl\_Constraint\_coefficient (ppl\_const\_Constraint\_t c, ppl\_dimension\_type var, ppl\_Coefficient\_t n)

Copies into n the coefficient of variable var in constraint c.

- int ppl\_Constraint\_inhomogeneous\_term (ppl\_const\_Constraint\_t c, ppl\_Coefficient\_t n) Copies into n the inhomogeneous term of constraint c.
- int ppl\_Constraint\_OK (ppl\_const\_Constraint\_t c)
  - Returns a positive integer if c is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if c is broken. Useful for debugging purposes.

# **Input/Output Functions**

 int ppl\_io\_print\_Constraint (ppl\_const\_Constraint\_t x) *Prints x to stdout.*

- int ppl\_io\_fprint\_Constraint (FILE \*stream, ppl\_const\_Constraint\_t x) *Prints x to the given output stream.*
- int ppl\_io\_asprint\_Constraint (char \*\*strp, ppl\_const\_Constraint\_t x)
   Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Constraint\_ascii\_dump (ppl\_const\_Constraint\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_Constraint\_ascii\_load (ppl\_Constraint\_t x, FILE \*stream) Loads an ascii representation of x from stream.

## 7.9.1 Detailed Description

Types and functions for constraints. The types and functions for constraints provide an interface towards *Constraint*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.10 ppl\_Generator\_System\_const\_iterator\_tag Interface Reference

Types and functions for iterating on generator systems.

```
#include <ppl_c_header.h>
```

# **Related Functions**

(Note that these are not member functions.)

## **Constructors, Assignment and Destructor**

- int ppl\_new\_Generator\_System\_const\_iterator (ppl\_Generator\_System\_const\_iterator\_t \*pgit) Builds a new 'const iterator' and writes a handle to it at address pgit.
- int ppl\_new\_Generator\_System\_const\_iterator\_from\_Generator\_System\_const\_iterator (ppl\_-Generator\_System\_const\_iterator\_t \*pgit, ppl\_const\_Generator\_System\_const\_iterator\_t git) Builds a const iterator that is a copy of git; writes a handle for the newly created const iterator at address pgit.
- int ppl\_assign\_Generator\_System\_const\_iterator\_from\_Generator\_System\_const\_iterator (ppl\_Generator\_System\_const\_iterator\_t dst, ppl\_const\_Generator\_System\_const\_iterator\_t src) Assigns a copy of the const iterator src to dst.
- int ppl\_delete\_Generator\_System\_const\_iterator (ppl\_const\_Generator\_System\_const\_iterator\_t git)

Invalidates the handle git: this makes sure the corresponding resources will eventually be released.

# Dereferencing, Incrementing and Equality Testing

The Parma Polyhedra Library C Language Interface User's Manual (version 0.11.2). See http://www.cs.unipr.it/ppl/ for more information.

• int ppl\_Generator\_System\_const\_iterator\_dereference (ppl\_const\_Generator\_System\_const\_iterator\_t git, ppl\_const\_Generator\_t \*pg)

Dereference git writing a const handle to the resulting generator at address pg.

• int ppl\_Generator\_System\_const\_iterator\_increment (ppl\_Generator\_System\_const\_iterator\_t git)

Increment git so that it "points" to the next generator.

• int ppl\_Generator\_System\_const\_iterator\_equal\_test (ppl\_const\_Generator\_System\_const\_iterator\_t x, ppl\_const\_Generator\_System\_const\_iterator\_t y) *Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.* 

#### 7.10.1 Detailed Description

Types and functions for iterating on generator systems. The types and functions for generator systems iterators provide read-only access to the elements of a generator system by interfacing *Generator\_System::const\_iterator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.11 ppl\_Generator\_System\_tag Interface Reference

Types and functions for generator systems.

```
#include <ppl_c_header.h>
```

## **Related Functions**

(Note that these are not member functions.)

## **Constructors, Assignment and Destructor**

- int ppl\_new\_Generator\_System (ppl\_Generator\_System\_t \*pgs) Builds an empty system of generators and writes a handle to it at address pgs.
- int ppl\_new\_Generator\_System\_from\_Generator (ppl\_Generator\_System\_t \*pgs, ppl\_const\_-Generator\_t g)

Builds the singleton generator system containing only a copy of generator g; writes a handle for the newly created system at address pgs.

 int ppl\_new\_Generator\_System\_from\_Generator\_System (ppl\_Generator\_System\_t \*pgs, ppl\_const\_Generator\_System\_t gs)

Builds a generator system that is a copy of gs; writes a handle for the newly created system at address pgs.

• int ppl\_assign\_Generator\_System\_from\_Generator\_System (ppl\_Generator\_System\_t dst, ppl\_const\_Generator\_System\_t src)

Assigns a copy of the generator system src to dst.

• int ppl\_delete\_Generator\_System (ppl\_const\_Generator\_System\_t gs) Invalidates the handle gs: this makes sure the corresponding resources will eventually be released.

### Functions that Do Not Modify the Generator System

 int ppl\_Generator\_System\_space\_dimension (ppl\_const\_Generator\_System\_t gs, ppl\_dimension\_type \*m)

Writes to m the dimension of the vector space enclosing gs.

- int ppl\_Generator\_System\_empty (ppl\_const\_Generator\_System\_t gs) Returns a positive integer if gs contains no generators; returns 0 otherwise.
- int ppl\_Generator\_System\_begin (ppl\_const\_Generator\_System\_t gs, ppl\_Generator\_System\_const\_iterator\_t git)

Assigns to git a const iterator "pointing" to the beginning of the generator system gs.

• int ppl\_Generator\_System\_end (ppl\_const\_Generator\_System\_t gs, ppl\_Generator\_System\_const\_iterator\_t git)

Assigns to git a const iterator "pointing" past the end of the generator system gs.

 int ppl\_Generator\_System\_OK (ppl\_const\_Generator\_System\_t gs) *Returns a positive integer if gs is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if gs is broken. Useful for debugging purposes.*

## Functions that May Modify the Generator System

- int ppl\_Generator\_System\_clear (ppl\_Generator\_System\_t gs) Removes all the generators from the generator system gs and sets its space dimension to 0.
- int ppl\_Generator\_System\_insert\_Generator (ppl\_Generator\_System\_t gs, ppl\_const\_-Generator\_t g)

Inserts a copy of the generator g into gs; the space dimension is increased, if necessary.

### **Input/Output Functions**

- int ppl\_io\_print\_Generator\_System (ppl\_const\_Generator\_System\_t x) Prints x to stdout.
- int ppl\_io\_fprint\_Generator\_System (FILE \*stream, ppl\_const\_Generator\_System\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_Generator\_System (char \*\*strp, ppl\_const\_Generator\_System\_t x) Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Generator\_System\_ascii\_dump (ppl\_const\_Generator\_System\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_Generator\_System\_ascii\_load (ppl\_Generator\_System\_t x, FILE \*stream) Loads an ascii representation of x from stream.

# 7.11.1 Detailed Description

Types and functions for generator systems. The types and functions for generator systems provide an interface towards *Generator\_System*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.12 ppl\_Generator\_tag Interface Reference

Types and functions for generators.

#include <ppl\_c\_header.h>

# **Related Functions**

(Note that these are not member functions.)

# **Constructors, Assignment and Destructor**

• int ppl\_new\_Generator (ppl\_Generator\_t \*pg, ppl\_const\_Linear\_Expression\_t le, enum ppl\_enum\_Generator\_Type t, ppl\_const\_Coefficient\_t d)

Creates a new generator of direction le and type t. If the generator to be created is a point or a closure point, the divisor d is applied to le. For other types of generators d is simply disregarded. A handle for the new generator is written at address pg. The space dimension of the new generator is equal to the space dimension of le.

• int ppl\_new\_Generator\_zero\_dim\_point (ppl\_Generator\_t \*pg)

*Creates the point that is the origin of the zero-dimensional space*  $\mathbb{R}^{0}$ *. Writes a handle for the new generator at address* pg.

• int ppl\_new\_Generator\_zero\_dim\_closure\_point (ppl\_Generator\_t \*pg)

*Creates, as a closure point, the point that is the origin of the zero-dimensional space*  $\mathbb{R}^{0}$ *. Writes a handle for the new generator at address pg.* 

- int ppl\_new\_Generator\_from\_Generator (ppl\_Generator\_t \*pg, ppl\_const\_Generator\_t g) Builds a generator that is a copy of g; writes a handle for the newly created generator at address pg.
- int ppl\_assign\_Generator\_from\_Generator (ppl\_Generator\_t dst, ppl\_const\_Generator\_t src) Assigns a copy of the generator src to dst.
- int ppl\_delete\_Generator (ppl\_const\_Generator\_t g) Invalidates the handle g: this makes sure the corresponding resources will eventually be released.

#### Functions that Do Not Modify the Generator

- int ppl\_Generator\_space\_dimension (ppl\_const\_Generator\_t g, ppl\_dimension\_type \*m) Writes to m the space dimension of g.
- int ppl\_Generator\_type (ppl\_const\_Generator\_t g) Returns the type of generator g.

int ppl\_Generator\_coefficient (ppl\_const\_Generator\_t g, ppl\_dimension\_type var, ppl\_Coefficient\_t n)

Copies into n the coefficient of variable var in generator g.

- int ppl\_Generator\_divisor (ppl\_const\_Generator\_t g, ppl\_Coefficient\_t n) If g is a point or a closure point assigns its divisor to n.
- int ppl\_Generator\_OK (ppl\_const\_Generator\_t g)
   *Returns a positive integer if g is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if g is broken. Useful for debugging purposes.*

# **Input/Output Functions**

- int ppl\_io\_print\_Generator (ppl\_const\_Generator\_t x)
   Prints x to stdout.
- int ppl\_io\_fprint\_Generator (FILE \*stream, ppl\_const\_Generator\_t x)
   Prints x to the given output stream.
- int ppl\_io\_asprint\_Generator (char \*\*strp, ppl\_const\_Generator\_t x)
   Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Generator\_ascii\_dump (ppl\_const\_Generator\_t x, FILE \*stream)
   Dumps an ascii representation of x on stream.
- int ppl\_Generator\_ascii\_load (ppl\_Generator\_t x, FILE \*stream) Loads an ascii representation of x from stream.

# 7.12.1 Detailed Description

Types and functions for generators. The types and functions for generators provide an interface towards *Generator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.13 ppl\_Grid\_Generator\_System\_const\_iterator\_tag Interface Reference

Types and functions for iterating on grid generator systems.

#include <ppl\_c\_header.h>

# **Related Functions**

(Note that these are not member functions.)

## **Constructors, Assignment and Destructor**

The Parma Polyhedra Library C Language Interface User's Manual (version 0.11.2). See http://www.cs.unipr.it/ppl/ for more information.

- int ppl\_new\_Grid\_Generator\_System\_const\_iterator (ppl\_Grid\_Generator\_System\_const\_iterator\_t \*pgit)
  - Builds a new 'const iterator' and writes a handle to it at address pgit.
- int ppl\_new\_Grid\_Generator\_System\_const\_iterator\_from\_Grid\_Generator\_System\_const\_iterator (ppl\_Grid\_Generator\_System\_const\_iterator\_t \*pgit, ppl\_const\_Grid\_Generator\_System\_const\_iterator\_t git)

Builds a const iterator that is a copy of git; writes a handle for the newly created const iterator at address pgit.

• int ppl\_assign\_Grid\_Generator\_System\_const\_iterator\_from\_Grid\_Generator\_System\_const\_iterator (ppl\_Grid\_Generator\_System\_const\_iterator\_t dst, ppl\_const\_Grid\_Generator\_System\_const\_iterator\_t src)

Assigns a copy of the const iterator src to dst.

• int ppl\_delete\_Grid\_Generator\_System\_const\_iterator (ppl\_const\_Grid\_Generator\_System\_const\_iterator\_t git)

Invalidates the handle git: this makes sure the corresponding resources will eventually be released.

# Dereferencing, Incrementing and Equality Testing

• int ppl\_Grid\_Generator\_System\_const\_iterator\_dereference (ppl\_const\_Grid\_Generator\_-System\_const\_iterator\_t git, ppl\_const\_Grid\_Generator\_t \*pg)

Dereference git writing a const handle to the resulting grid generator at address pg.

• int ppl\_Grid\_Generator\_System\_const\_iterator\_increment (ppl\_Grid\_Generator\_System\_const\_iterator\_t git)

Increment git so that it "points" to the next grid generator.

• int ppl\_Grid\_Generator\_System\_const\_iterator\_equal\_test (ppl\_const\_Grid\_Generator\_-System\_const\_iterator\_t x, ppl\_const\_Grid\_Generator\_System\_const\_iterator\_t y) *Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.* 

# 7.13.1 Detailed Description

Types and functions for iterating on grid generator systems. The types and functions for grid generator systems iterators provide read-only access to the elements of a grid generator system by interfacing *Grid\_Generator\_System::const\_iterator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.14 ppl\_Grid\_Generator\_System\_tag Interface Reference

Types and functions for grid generator systems.

#include <ppl\_c\_header.h>

# **Related Functions**

(Note that these are not member functions.)

#### **Constructors, Assignment and Destructor**

- int ppl\_new\_Grid\_Generator\_System (ppl\_Grid\_Generator\_System\_t \*pgs) Builds an empty system of grid generators and writes a handle to it at address pgs.
- int ppl\_new\_Grid\_Generator\_System\_from\_Grid\_Generator (ppl\_Grid\_Generator\_System\_t \*pgs, ppl\_const\_Grid\_Generator\_t g)

Builds the singleton grid generator system containing only a copy of generator g; writes a handle for the newly created system at address pgs.

int ppl\_new\_Grid\_Generator\_System\_from\_Grid\_Generator\_System (ppl\_Grid\_Generator\_System\_t \*pgs, ppl\_const\_Grid\_Generator\_System\_t gs)

Builds a grid generator system that is a copy of gs; writes a handle for the newly created system at address pgs.

- int ppl\_assign\_Grid\_Generator\_System\_from\_Grid\_Generator\_System (ppl\_Grid\_Generator\_ System\_t dst, ppl\_const\_Grid\_Generator\_System\_t src) Assigns a copy of the grid generator system src to dst.
- int ppl\_delete\_Grid\_Generator\_System (ppl\_const\_Grid\_Generator\_System\_t gs) Invalidates the handle gs: this makes sure the corresponding resources will eventually be released.

#### Functions that Do Not Modify the Grid Generator System

int ppl\_Grid\_Generator\_System\_space\_dimension (ppl\_const\_Grid\_Generator\_System\_t gs, ppl\_dimension\_type \*m)
 Writes to m the dimension of the vector space analoging go.

Writes to m the dimension of the vector space enclosing gs.

- int ppl\_Grid\_Generator\_System\_empty (ppl\_const\_Grid\_Generator\_System\_t gs) Returns a positive integer if gs contains no generator; returns 0 otherwise.
- int ppl\_Grid\_Generator\_System\_begin (ppl\_const\_Grid\_Generator\_System\_t gs, ppl\_Grid\_-Generator\_System\_const\_iterator\_t git) Assigns to git a const iterator "pointing" to the beginning of the grid generator system gs.
- int ppl\_Grid\_Generator\_System\_end (ppl\_const\_Grid\_Generator\_System\_t gs, ppl\_Grid\_-Generator\_System\_const\_iterator\_t git)

Assigns to git a const iterator "pointing" past the end of the grid generator system gs.

 int ppl\_Grid\_Generator\_System\_OK (ppl\_const\_Grid\_Generator\_System\_t gs) *Returns a positive integer if gs is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if gs is broken. Useful for debugging purposes.*

# Functions that May Modify the Grid Generator System

• int ppl\_Grid\_Generator\_System\_clear (ppl\_Grid\_Generator\_System\_t gs) Removes all the generators from the grid generator system gs and sets its space dimension to 0.

- int ppl\_Grid\_Generator\_System\_insert\_Grid\_Generator (ppl\_Grid\_Generator\_System\_t gs, ppl\_const\_Grid\_Generator\_t g)
  - Inserts a copy of the grid generator g into gs; the space dimension is increased, if necessary.

#### **Input/Output Functions**

- int ppl\_io\_print\_Grid\_Generator\_System (ppl\_const\_Grid\_Generator\_System\_t x) Prints x to stdout.
- int ppl\_io\_fprint\_Grid\_Generator\_System (FILE \*stream, ppl\_const\_Grid\_Generator\_System\_t x)
   Prints x to the given output stream.
- int ppl io asprint Grid Generator System (char \*\*strp, ppl const Grid Generator System t x)

Prints x to a malloc-allocated string, a pointer to which is returned via strp.

• int ppl\_Grid\_Generator\_System\_ascii\_dump (ppl\_const\_Grid\_Generator\_System\_t x, FILE \*stream)

Dumps an ascii representation of x on stream.

• int ppl\_Grid\_Generator\_System\_ascii\_load (ppl\_Grid\_Generator\_System\_t x, FILE \*stream) Loads an ascii representation of x from stream.

## 7.14.1 Detailed Description

Types and functions for grid generator systems. The types and functions for grid generator systems provide an interface towards *Grid\_Generator\_System*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.15 ppl\_Grid\_Generator\_tag Interface Reference

Types and functions for grid generators.

```
#include <ppl_c_header.h>
```

# **Related Functions**

(Note that these are not member functions.)

#### **Constructors, Assignment and Destructor**

• int ppl\_new\_Grid\_Generator (ppl\_Grid\_Generator\_t \*pg, ppl\_const\_Linear\_Expression\_t le, enum ppl\_enum\_Grid\_Generator\_Type t, ppl\_const\_Coefficient\_t d)

Creates a new grid generator of direction  $l \in$  and type t. If the grid generator to be created is a point or a parameter, the divisor d is applied to  $l \in$ . If it is a line, d is simply disregarded. A handle for the new grid generator is written at address pg. The space dimension of the new grid generator is equal to the space dimension of  $l \in$ .

- int ppl\_new\_Grid\_Generator\_zero\_dim\_point (ppl\_Grid\_Generator\_t \*pg)
   Creates the point that is the origin of the zero-dimensional space R<sup>0</sup>. Writes a handle for the new grid generator at address pg.
- int ppl\_new\_Grid\_Generator\_from\_Grid\_Generator (ppl\_Grid\_Generator\_t \*pg, ppl\_const\_-Grid\_Generator\_t g)

Builds a grid generator that is a copy of g; writes a handle for the newly created grid generator at address pg.

• int ppl\_assign\_Grid\_Generator\_from\_Grid\_Generator (ppl\_Grid\_Generator\_t dst, ppl\_const\_Grid\_Generator\_t src)

Assigns a copy of the grid generator src to dst.

• int ppl\_delete\_Grid\_Generator (ppl\_const\_Grid\_Generator\_t g) Invalidates the handle g: this makes sure the corresponding resources will eventually be released.

## Functions that Do Not Modify the Grid Generator

int ppl\_Grid\_Generator\_space\_dimension (ppl\_const\_Grid\_Generator\_t g, ppl\_dimension\_type \*m)

Writes to m the space dimension of g.

- int ppl\_Grid\_Generator\_type (ppl\_const\_Grid\_Generator\_t g) *Returns the type of grid generator g.*
- int ppl\_Grid\_Generator\_coefficient (ppl\_const\_Grid\_Generator\_t g, ppl\_dimension\_type var, ppl\_Coefficient\_t n)

Copies into n the coefficient of variable var in grid generator g.

- int ppl\_Grid\_Generator\_divisor (ppl\_const\_Grid\_Generator\_t g, ppl\_Coefficient\_t n) If g is a point or a parameter assigns its divisor to n.
- int ppl\_Grid\_Generator\_OK (ppl\_const\_Grid\_Generator\_t g) *Returns a positive integer if g is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if g is broken. Useful for debugging purposes.*

# **Input/Output Functions**

- int ppl\_io\_print\_Grid\_Generator (ppl\_const\_Grid\_Generator\_t x) Prints x to stdout.
- int ppl\_io\_fprint\_Grid\_Generator (FILE \*stream, ppl\_const\_Grid\_Generator\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_Grid\_Generator (char \*\*strp, ppl\_const\_Grid\_Generator\_t x) Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Grid\_Generator\_ascii\_dump (ppl\_const\_Grid\_Generator\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_Grid\_Generator\_ascii\_load (ppl\_Grid\_Generator\_t x, FILE \*stream) Loads an ascii representation of x from stream.

## 7.15.1 Detailed Description

Types and functions for grid generators. The types and functions for grid generators provide an interface towards *Grid\_Generator*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.16 ppl\_Linear\_Expression\_tag Interface Reference

Types and functions for linear expressions.

#include <ppl\_c\_header.h>

#### **Related Functions**

(Note that these are not member functions.)

#### **Constructors, Assignment and Destructor**

• int ppl\_new\_Linear\_Expression (ppl\_Linear\_Expression\_t \*ple)

*Creates a new linear expression corresponding to the constant 0 in a zero-dimensional space; writes a handle for the new linear expression at address ple.* 

 int ppl\_new\_Linear\_Expression\_with\_dimension (ppl\_Linear\_Expression\_t \*ple, ppl\_dimension\_type d)

Creates a new linear expression corresponding to the constant 0 in a d-dimensional space; writes a handle for the new linear expression at address ple.

• int ppl\_new\_Linear\_Expression\_from\_Linear\_Expression (ppl\_Linear\_Expression\_t \*ple, ppl\_const\_Linear\_Expression\_t le)

Builds a linear expression that is a copy of 1e; writes a handle for the newly created linear expression at address ple.

 int ppl\_new\_Linear\_Expression\_from\_Constraint (ppl\_Linear\_Expression\_t \*ple, ppl\_const\_-Constraint\_t c)

Builds a linear expression corresponding to constraint c; writes a handle for the newly created linear expression at address ple.

• int ppl\_new\_Linear\_Expression\_from\_Generator (ppl\_Linear\_Expression\_t \*ple, ppl\_const\_-Generator\_t g)

Builds a linear expression corresponding to generator g; writes a handle for the newly created linear expression at address ple.

 int ppl\_new\_Linear\_Expression\_from\_Congruence (ppl\_Linear\_Expression\_t \*ple, ppl\_const\_-Congruence\_t c)

Builds a linear expression corresponding to congruence c; writes a handle for the newly created linear expression at address ple.

• int ppl\_new\_Linear\_Expression\_from\_Grid\_Generator (ppl\_Linear\_Expression\_t \*ple, ppl\_const\_Grid\_Generator\_t g)

Builds a linear expression corresponding to grid generator g; writes a handle for the newly created linear expression at address ple.

• int ppl\_assign\_Linear\_Expression\_from\_Linear\_Expression (ppl\_Linear\_Expression\_t dst, ppl\_const\_Linear\_Expression\_t src)

Assigns a copy of the linear expression src to dst.

• int ppl\_delete\_Linear\_Expression (ppl\_const\_Linear\_Expression\_t le) Invalidates the handle le: this makes sure the corresponding resources will eventually be released.

## Functions that Do Not Modify the Linear Expression

 int ppl\_Linear\_Expression\_space\_dimension (ppl\_const\_Linear\_Expression\_t le, ppl\_dimension\_type \*m)

Writes to m the space dimension of le.

• int ppl\_Linear\_Expression\_coefficient (ppl\_const\_Linear\_Expression\_t le, ppl\_dimension\_type var, ppl\_Coefficient\_t n)

Copies into n the coefficient of variable var in the linear expression le.

• int ppl\_Linear\_Expression\_inhomogeneous\_term (ppl\_const\_Linear\_Expression\_t le, ppl\_Coefficient\_t n)

Copies into n the inhomogeneous term of linear expression le.

- int ppl\_Linear\_Expression\_OK (ppl\_const\_Linear\_Expression\_t le) *Returns a positive integer if le is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if le is broken. Useful for debugging purposes.*
- int ppl\_Linear\_Expression\_is\_zero (ppl\_const\_Linear\_Expression\_t le) Returns true if and only if \*this is 0.
- int ppl\_Linear\_Expression\_all\_homogeneous\_terms\_are\_zero (ppl\_const\_Linear\_Expression\_t le)

Returns true if and only if all the homogeneous terms of \*this are 0.

## Functions that May Modify the Linear Expression

• int ppl\_Linear\_Expression\_add\_to\_coefficient (ppl\_Linear\_Expression\_t le, ppl\_dimension\_type var, ppl\_const\_Coefficient\_t n)

Adds n to the coefficient of variable var in the linear expression le. The space dimension is set to be the maximum between var + 1 and the old space dimension.

• int ppl\_Linear\_Expression\_add\_to\_inhomogeneous (ppl\_Linear\_Expression\_t le, ppl\_const\_Coefficient\_t n)

Adds n to the inhomogeneous term of the linear expression le.

- int ppl\_add\_Linear\_Expression\_to\_Linear\_Expression (ppl\_Linear\_Expression\_t dst, ppl\_const\_Linear\_Expression\_t src)
   Adds the linear expression src to dst.
- int ppl\_subtract\_Linear\_Expression\_from\_Linear\_Expression (ppl\_Linear\_Expression\_t dst, ppl\_const\_Linear\_Expression\_t src)

Subtracts the linear expression src from dst.

• int ppl\_multiply\_Linear\_Expression\_by\_Coefficient (ppl\_Linear\_Expression\_t le, ppl\_const\_Coefficient\_t n)

Multiply the linear expression dst by n.

# **Input/Output Functions**

- int ppl\_io\_print\_Linear\_Expression (ppl\_const\_Linear\_Expression\_t x) Prints x to stdout.
- int ppl\_io\_fprint\_Linear\_Expression (FILE \*stream, ppl\_const\_Linear\_Expression\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_Linear\_Expression (char \*\*strp, ppl\_const\_Linear\_Expression\_t x) Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Linear\_Expression\_ascii\_dump (ppl\_const\_Linear\_Expression\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_Linear\_Expression\_ascii\_load (ppl\_Linear\_Expression\_t x, FILE \*stream) Loads an ascii representation of x from stream.

# 7.16.1 Detailed Description

Types and functions for linear expressions. The types and functions for linear expression provide an interface towards *Linear\_Expression*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.17 ppl\_MIP\_Problem\_tag Interface Reference

Types and functions for MIP problems.

#include <ppl\_c\_header.h>

# **Related Functions**

(Note that these are not member functions.)

## Symbolic Constants

- int PPL\_OPTIMIZATION\_MODE\_MAXIMIZATION Code of the "maximization" optimization mode.
- int PPL\_OPTIMIZATION\_MODE\_MINIMIZATION Code of the "minimization" optimization mode.
- int PPL\_MIP\_PROBLEM\_STATUS\_UNFEASIBLE

Code of the "unfeasible MIP problem" status.

- int PPL\_MIP\_PROBLEM\_STATUS\_UNBOUNDED Code of the "unbounded MIP problem" status.
- int PPL\_MIP\_PROBLEM\_STATUS\_OPTIMIZED Code of the "optimized MIP problem" status.
- int PPL\_MIP\_PROBLEM\_CONTROL\_PARAMETER\_NAME\_PRICING Code for the MIP problem's "pricing" control parameter name.
- int PPL\_MIP\_PROBLEM\_CONTROL\_PARAMETER\_PRICING\_TEXTBOOK Code of MIP problem's "textbook" pricing method.
- int PPL\_MIP\_PROBLEM\_CONTROL\_PARAMETER\_PRICING\_STEEPEST\_EDGE\_EXACT

Code of MIP problem's "exact steepest-edge" pricing method.

• int PPL\_MIP\_PROBLEM\_CONTROL\_PARAMETER\_PRICING\_STEEPEST\_EDGE\_FLOAT Code of MIP problem's "float steepest-edge" pricing method.

## **Constructors, Assignment and Destructor**

- int ppl\_new\_MIP\_Problem\_from\_space\_dimension (ppl\_MIP\_Problem\_t \*pmip, ppl\_-dimension\_type d)
   Builds a trivial MIP problem of dimension d and writes a handle to it at address pmip.
- int ppl\_new\_MIP\_Problem (ppl\_MIP\_Problem\_t \*pmip, ppl\_dimension\_type d, ppl\_const\_-Constraint\_System\_t cs, ppl\_const\_Linear\_Expression\_t le, int m)

Builds a MIP problem of space dimension d having feasible region cs, objective function le and optimization mode m; writes a handle to it at address pmip.

• int ppl\_new\_MIP\_Problem\_from\_MIP\_Problem (ppl\_MIP\_Problem\_t \*pmip, ppl\_const\_MIP\_Problem\_t mip)

Builds a MIP problem that is a copy of mip; writes a handle for the newly created system at address pmip.

• int ppl\_assign\_MIP\_Problem\_from\_MIP\_Problem (ppl\_MIP\_Problem\_t dst, ppl\_const\_MIP\_Problem\_t src)

Assigns a copy of the MIP problem src to dst.

• int ppl\_delete\_MIP\_Problem (ppl\_const\_MIP\_Problem\_t mip) Invalidates the handle mip: this makes sure the corresponding resources will eventually be released.

#### Functions that Do Not Modify the MIP\_Problem

int ppl\_MIP\_Problem\_space\_dimension (ppl\_const\_MIP\_Problem\_t mip, ppl\_dimension\_type \*m)

Writes to m the dimension of the vector space enclosing mip.

int ppl\_MIP\_Problem\_number\_of\_integer\_space\_dimensions (ppl\_const\_MIP\_Problem\_t mip, ppl\_dimension\_type \*m)

Writes to m the number of integer space dimensions of mip.

- int ppl\_MIP\_Problem\_integer\_space\_dimensions (ppl\_const\_MIP\_Problem\_t mip, ppl\_dimension\_type ds[])
  - Writes in the first positions of the array ds all the integer space dimensions of problem mip. If the array is not big enough to hold all of the integer space dimensions, the behavior is undefined.
- int ppl\_MIP\_Problem\_number\_of\_constraints (ppl\_const\_MIP\_Problem\_t mip, ppl\_dimension\_type \*m)

Writes to m the number of constraints defining the feasible region of mip.

• int ppl\_MIP\_Problem\_constraint\_at\_index (ppl\_const\_MIP\_Problem\_t mip, ppl\_dimension\_type i, ppl\_const\_Constraint\_t \*pc)

Writes at address pc a const handle to the i-th constraint defining the feasible region of the MIP problem mip.

 int ppl\_MIP\_Problem\_objective\_function (ppl\_const\_MIP\_Problem\_t mip, ppl\_const\_Linear\_-Expression\_t \*ple)

Writes a const handle to the linear expression defining the objective function of the MIP problem mip at address ple.

- int ppl\_MIP\_Problem\_optimization\_mode (ppl\_const\_MIP\_Problem\_t mip) Returns the optimization mode of the MIP problem mip.
- int ppl\_MIP\_Problem\_OK (ppl\_const\_MIP\_Problem\_t mip) *Returns a positive integer if mip is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if mip is broken. Useful for debugging purposes.*

#### Functions that May Modify the MIP\_Problem

- int ppl\_MIP\_Problem\_clear (ppl\_MIP\_Problem\_t mip) Resets the MIP problem to be a trivial problem of space dimension 0.
- int ppl\_MIP\_Problem\_add\_space\_dimensions\_and\_embed (ppl\_MIP\_Problem\_t mip, ppl\_dimension\_type d)

Adds d new dimensions to the space enclosing the MIP problem mip and to mip itself.

• int ppl\_MIP\_Problem\_add\_to\_integer\_space\_dimensions (ppl\_MIP\_Problem\_t mip, ppl\_dimension\_type ds[], size\_t n)

Sets the space dimensions that are specified in first n positions of the array ds to be integer dimensions of problem mip. The presence of duplicates in ds is a waste but an innocuous one.

- int ppl\_MIP\_Problem\_add\_constraint (ppl\_MIP\_Problem\_t mip, ppl\_const\_Constraint\_t c) Modifies the feasible region of the MIP problem mip by adding a copy of the constraint c.
- int ppl\_MIP\_Problem\_add\_constraints (ppl\_MIP\_Problem\_t mip, ppl\_const\_Constraint\_-System\_t cs)

Modifies the feasible region of the MIP problem mip by adding a copy of the constraints in cs.

• int ppl\_MIP\_Problem\_set\_objective\_function (ppl\_MIP\_Problem\_t mip, ppl\_const\_Linear\_Expression\_t le)

Sets the objective function of the MIP problem mip to a copy of le.

• int ppl\_MIP\_Problem\_set\_optimization\_mode (ppl\_MIP\_Problem\_t mip, int mode) Sets the optimization mode of the MIP problem mip to mode.

#### Computing the Solution of the MIP\_Problem

- int ppl\_MIP\_Problem\_is\_satisfiable (ppl\_const\_MIP\_Problem\_t mip) Returns a positive integer if mip is satisfiable; returns 0 otherwise.
- int ppl\_MIP\_Problem\_solve (ppl\_const\_MIP\_Problem\_t mip) Solves the MIP problem mip, returning an exit status.
- int ppl\_MIP\_Problem\_evaluate\_objective\_function (ppl\_const\_MIP\_Problem\_t mip, ppl\_const\_Generator\_t g, ppl\_Coefficient\_t num, ppl\_Coefficient\_t den)
   Evaluates the objective function of mip on point g.
- int ppl\_MIP\_Problem\_feasible\_point (ppl\_const\_MIP\_Problem\_t mip, ppl\_const\_Generator\_t \*pg)

Writes a const handle to a feasible point for the MIP problem mip at address pg.

int ppl\_MIP\_Problem\_optimizing\_point (ppl\_const\_MIP\_Problem\_t mip, ppl\_const\_Generator\_t \*pg)
 Writes a const han the set of the MID problem raise at address a rest.

Writes a const handle to an optimizing point for the MIP problem mip at address pg.

int ppl\_MIP\_Problem\_optimal\_value (ppl\_const\_MIP\_Problem\_t mip, ppl\_Coefficient\_t num, ppl\_Coefficient\_t den)

Returns the optimal value for mip.

#### **Querying/Setting Control Parameters**

- int ppl\_MIP\_Problem\_get\_control\_parameter (ppl\_const\_MIP\_Problem\_t mip, int name) Returns the value of control parameter name in problem mip.
- int ppl\_MIP\_Problem\_set\_control\_parameter (ppl\_MIP\_Problem\_t mip, int value) Sets control parameter value in problem mip.
- int ppl\_MIP\_Problem\_total\_memory\_in\_bytes (ppl\_const\_MIP\_Problem\_t mip, size\_t \*sz) Writes into \*sz the size in bytes of the memory occupied by mip.
- int ppl\_MIP\_Problem\_external\_memory\_in\_bytes (ppl\_const\_MIP\_Problem\_t mip, size\_t \*sz) Writes into \*sz the size in bytes of the memory managed by mip.

## **Input/Output Functions**

- int ppl\_io\_print\_MIP\_Problem (ppl\_const\_MIP\_Problem\_t x) Prints x to stdout.
- int ppl\_io\_fprint\_MIP\_Problem (FILE \*stream, ppl\_const\_MIP\_Problem\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_MIP\_Problem (char \*\*strp, ppl\_const\_MIP\_Problem\_t x)

Prints x to a malloc-allocated string, a pointer to which is returned via strp.

- int ppl\_MIP\_Problem\_ascii\_dump (ppl\_const\_MIP\_Problem\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_MIP\_Problem\_ascii\_load (ppl\_MIP\_Problem\_t x, FILE \*stream) Loads an ascii representation of x from stream.

## 7.17.1 Detailed Description

Types and functions for MIP problems. The types and functions for MIP problems provide an interface towards *MIP\_Problem*.

# 7.17.2 Friends And Related Function Documentation

## 7.17.2.1 int ppl\_MIP\_Problem\_solve (ppl\_const\_MIP\_Problem\_t mip) [related]

Solves the MIP problem mip, returning an exit status.

# Returns

PPL\_MIP\_PROBLEM\_STATUS\_UNFEASIBLE if the MIP problem is not satisfiable; PPL\_MIP\_-PROBLEM\_STATUS\_UNBOUNDED if the MIP problem is satisfiable but there is no finite bound to the value of the objective function; PPL\_MIP\_PROBLEM\_STATUS\_OPTIMIZED if the MIP problem admits an optimal solution.

# 7.17.2.2 int ppl\_MIP\_Problem\_evaluate\_objective\_function (ppl\_const\_MIP\_Problem\_t *mip*, ppl\_const\_Generator\_t g, ppl\_Coefficient\_t *num*, ppl\_Coefficient\_t *den*) [related]

Evaluates the objective function of mip on point g.

# Parameters

*mip* The MIP problem defining the objective function;

- **g** The generator on which the objective function will be evaluated;
- num Will be assigned the numerator of the objective function value;
- den Will be assigned the denominator of the objective function value;

# 7.17.2.3 int ppl\_MIP\_Problem\_optimal\_value (ppl\_const\_MIP\_Problem\_t *mip*, ppl\_Coefficient\_t *num*, ppl\_Coefficient\_t *den*) [related]

Returns the optimal value for mip.

## **Parameters**

*mip* The MIP problem;

num Will be assigned the numerator of the optimal value;

*den* Will be assigned the denominator of the optimal value.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.18 ppl\_PIP\_Decision\_Node\_tag Interface Reference

Types and functions for PIP decision nodes.

```
#include <ppl_c_header.h>
```

# **Related Functions**

(Note that these are not member functions.)

int ppl\_PIP\_Decision\_Node\_get\_child\_node (ppl\_const\_PIP\_Decision\_Node\_t pip\_dec, int b, ppl\_const\_PIP\_Tree\_Node\_t \*pip\_tree)

Writes to pip\_tree a const pointer to either the true branch (if b is not zero) or the false branch (if b is zero) of pip\_dec.

# **Input/Output Functions**

- int ppl\_io\_print\_PIP\_Decision\_Node (ppl\_const\_PIP\_Decision\_Node\_t x) Prints x to stdout.
- int ppl\_io\_fprint\_PIP\_Decision\_Node (FILE \*stream, ppl\_const\_PIP\_Decision\_Node\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_PIP\_Decision\_Node (char \*\*strp, ppl\_const\_PIP\_Decision\_Node\_t x) Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_PIP\_Decision\_Node\_ascii\_dump (ppl\_const\_PIP\_Decision\_Node\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_PIP\_Decision\_Node\_ascii\_load (ppl\_PIP\_Decision\_Node\_t x, FILE \*stream) Loads an ascii representation of x from stream.

## 7.18.1 Detailed Description

Types and functions for PIP decision nodes. The types and functions for decision nodes provide an interface towards *PIP\_Decision\_Node*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.19 ppl\_PIP\_Problem\_tag Interface Reference

Types and functions for PIP problems.

#include <ppl\_c\_header.h>

## **Related Functions**

(Note that these are not member functions.)

## Symbolic Constants

- int PPL\_PIP\_PROBLEM\_STATUS\_UNFEASIBLE Code of the "unfeasible PIP problem" status.
- int PPL\_PIP\_PROBLEM\_STATUS\_OPTIMIZED Code of the "optimized PIP problem" status.
- int PPL\_PIP\_PROBLEM\_CONTROL\_PARAMETER\_NAME\_CUTTING\_STRATEGY Code for the PIP problem's "cutting strategy" control parameter name.
- int PPL\_PIP\_PROBLEM\_CONTROL\_PARAMETER\_NAME\_PIVOT\_ROW\_STRATEGY Code for the PIP problem's "pivot row strategy" control parameter name.
- int PPL\_PIP\_PROBLEM\_CONTROL\_PARAMETER\_CUTTING\_STRATEGY\_FIRST Code of PIP problem's "first" cutting strategy.
- int PPL\_PIP\_PROBLEM\_CONTROL\_PARAMETER\_CUTTING\_STRATEGY\_DEEPEST Code of PIP problem's "deepest" cutting strategy.
- int PPL\_PIP\_PROBLEM\_CONTROL\_PARAMETER\_CUTTING\_STRATEGY\_ALL Code of PIP problem's "all" cutting strategy.
- int PPL\_PIP\_PROBLEM\_CONTROL\_PARAMETER\_PIVOT\_ROW\_STRATEGY\_FIRST Code of PIP problem's "first" pivot row strategy.
- int PPL\_PIP\_PROBLEM\_CONTROL\_PARAMETER\_PIVOT\_ROW\_STRATEGY\_MAX\_-COLUMN

Code of PIP problem's "max column" pivot row strategy.

## **Constructors, Assignment and Destructor**

 int ppl\_new\_PIP\_Problem\_from\_space\_dimension (ppl\_PIP\_Problem\_t \*ppip, ppl\_dimension\_type d)

Builds a trivial PIP problem of dimension d and writes a handle to it at address ppip.

• int ppl\_new\_PIP\_Problem\_from\_PIP\_Problem (ppl\_PIP\_Problem\_t \*ppip, ppl\_const\_PIP\_Problem\_t pip)

Builds a PIP problem that is a copy of pip; writes a handle for the newly created problem at address ppip.

• int ppl\_assign\_PIP\_Problem\_from\_PIP\_Problem (ppl\_PIP\_Problem\_t dst, ppl\_const\_PIP\_Problem\_t src)

Assigns a copy of the PIP problem src to dst.

• int ppl\_new\_PIP\_Problem\_from\_constraints (ppl\_PIP\_Problem\_t \*ppip, ppl\_dimension\_type d, ppl\_Constraint\_System\_const\_iterator\_t first, ppl\_Constraint\_System\_const\_iterator\_t last, size\_t n, ppl\_dimension\_type ds[])

Builds a PIP problem having space dimension d from the sequence of constraints in the range [first, last); the n dimensions whose indices occur in ds are interpreted as parameters.

• int ppl\_delete\_PIP\_Problem (ppl\_const\_PIP\_Problem\_t pip)

Invalidates the handle pip: this makes sure the corresponding resources will eventually be released.

#### Functions that Do Not Modify the PIP\_Problem

int ppl\_PIP\_Problem\_space\_dimension (ppl\_const\_PIP\_Problem\_t pip, ppl\_dimension\_type \*m)

Writes to m the dimension of the vector space enclosing pip.

• int ppl\_PIP\_Problem\_number\_of\_parameter\_space\_dimensions (ppl\_const\_PIP\_Problem\_t pip, ppl\_dimension\_type \*m)

Writes to m the number of parameter space dimensions of pip.

• int ppl\_PIP\_Problem\_parameter\_space\_dimensions (ppl\_const\_PIP\_Problem\_t pip, ppl\_dimension\_type ds[])

Writes in the first positions of the array ds all the parameter space dimensions of problem pip. If the array is not big enough to hold all of the parameter space dimensions, the behavior is undefined.

 int ppl\_PIP\_Problem\_get\_big\_parameter\_dimension (ppl\_const\_PIP\_Problem\_t pip, ppl\_dimension\_type \*pd)

Writes into \*pd the big parameter dimension of PIP problem pip.

• int ppl\_PIP\_Problem\_number\_of\_constraints (ppl\_const\_PIP\_Problem\_t pip, ppl\_dimension\_type \*m)

Writes to m the number of constraints defining the feasible region of pip.

• int ppl\_PIP\_Problem\_constraint\_at\_index (ppl\_const\_PIP\_Problem\_t pip, ppl\_dimension\_type i, ppl\_const\_Constraint\_t \*pc)

Writes at address pc a const handle to the i-th constraint defining the feasible region of the PIP problem pip.

- int ppl\_PIP\_Problem\_total\_memory\_in\_bytes (ppl\_const\_PIP\_Problem\_t pip, size\_t \*sz) Writes into \*sz the size in bytes of the memory occupied by pip.
- int ppl\_PIP\_Problem\_external\_memory\_in\_bytes (ppl\_const\_PIP\_Problem\_t pip, size\_t \*sz) Writes into \*sz the size in bytes of the memory managed by pip.
- int ppl\_PIP\_Problem\_OK (ppl\_const\_PIP\_Problem\_t pip) *Returns a positive integer if pip is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if pip is broken. Useful for debugging purposes.*

#### Functions that May Modify the PIP\_Problem

• int ppl\_PIP\_Problem\_clear (ppl\_PIP\_Problem\_t pip)

Resets the PIP problem to be a trivial problem of space dimension 0.

• int ppl\_PIP\_Problem\_add\_space\_dimensions\_and\_embed (ppl\_PIP\_Problem\_t pip, ppl\_dimension\_type pip\_vars, ppl\_dimension\_type pip\_params)

Adds pip\_vars + pip\_params new space dimensions and embeds the PIP problem pip in the new vector space.

• int ppl\_PIP\_Problem\_add\_to\_parameter\_space\_dimensions (ppl\_PIP\_Problem\_t pip, ppl\_dimension\_type ds[], size\_t n)

```
Sets the space dimensions that are specified in first n positions of the array ds to be parameter dimensions of problem pip. The presence of duplicates in ds is a waste but an innocuous one.
```

• int ppl\_PIP\_Problem\_set\_big\_parameter\_dimension (ppl\_PIP\_Problem\_t pip, ppl\_dimension\_type d)

Sets the big parameter dimension of PIP problem pip to d.

- int ppl\_PIP\_Problem\_add\_constraint (ppl\_PIP\_Problem\_t pip, ppl\_const\_Constraint\_t c) Modifies the feasible region of the PIP problem pip by adding a copy of the constraint c.
- int ppl\_PIP\_Problem\_add\_constraints (ppl\_PIP\_Problem\_t pip, ppl\_const\_Constraint\_System\_t cs)

Modifies the feasible region of the PIP problem pip by adding a copy of the constraints in cs.

## Computing and Printing the Solution of the PIP\_Problem

- int ppl\_PIP\_Problem\_is\_satisfiable (ppl\_const\_PIP\_Problem\_t pip) Returns a positive integer if pip is satisfiable and an optimal solution can be found; returns 0 otherwise.
- int ppl\_PIP\_Problem\_solve (ppl\_const\_PIP\_Problem\_t pip) Solves the PIP problem pip, returning an exit status.
- int ppl\_PIP\_Problem\_solution (ppl\_const\_PIP\_Problem\_t pip, ppl\_const\_PIP\_Tree\_Node\_t \*pip\_tree)

Writes to pip\_tree a solution for pip, if it exists.

 int ppl\_PIP\_Problem\_optimizing\_solution (ppl\_const\_PIP\_Problem\_t pip, ppl\_const\_PIP\_Tree\_-Node\_t \*pip\_tree)

Writes to pip\_tree an optimizing solution for pip, if it exists.

# **Querying/Setting Control Parameters**

- int ppl\_PIP\_Problem\_get\_control\_parameter (ppl\_const\_PIP\_Problem\_t pip, int name) Returns the value of control parameter name in problem pip.
- int ppl\_PIP\_Problem\_set\_control\_parameter (ppl\_PIP\_Problem\_t pip, int value) Sets control parameter value in problem pip.

## **Input/Output Functions**

• int ppl\_io\_print\_PIP\_Problem (ppl\_const\_PIP\_Problem\_t x) Prints x to stdout.

- int ppl\_io\_fprint\_PIP\_Problem (FILE \*stream, ppl\_const\_PIP\_Problem\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_PIP\_Problem (char \*\*strp, ppl\_const\_PIP\_Problem\_t x) Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_PIP\_Problem\_ascii\_dump (ppl\_const\_PIP\_Problem\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_PIP\_Problem\_ascii\_load (ppl\_PIP\_Problem\_t x, FILE \*stream) Loads an ascii representation of x from stream.

## 7.19.1 Detailed Description

Types and functions for PIP problems. The types and functions for PIP problems provide an interface towards *PIP\_Problem*.

## 7.19.2 Friends And Related Function Documentation

# 7.19.2.1 int ppl\_PIP\_Problem\_space\_dimension (ppl\_const\_PIP\_Problem\_t *pip*, ppl\_dimension\_type \* *m*) [related]

Writes to m the dimension of the vector space enclosing pip.

The vector space dimensions includes both the problem variables and the problem parameters, but they do not include the artificial parameters.

# 7.19.2.2 int ppl\_PIP\_Problem\_add\_space\_dimensions\_and\_embed (ppl\_PIP\_Problem\_t *pip*, ppl\_dimension\_type *pip\_vars*, ppl\_dimension\_type *pip\_params*) [related]

Adds pip\_vars + pip\_params new space dimensions and embeds the PIP problem pip in the new vector space.

# Parameters

- *pip* The PIP problem to be embedded in the new vector space.
- pip\_vars The number of space dimensions to add that are interpreted as PIP problem variables (i.e., non parameters). These are added before adding the pip\_params parameters.
- *pip\_params* The number of space dimensions to add that are interpreted as PIP problem parameters. These are added *after* having added the pip\_vars problem variables.

The new space dimensions will be those having the highest indexes in the new PIP problem; they are initially unconstrained.

# 7.19.2.3 int ppl\_PIP\_Problem\_solve (ppl\_const\_PIP\_Problem\_t pip) [related]

Solves the PIP problem pip, returning an exit status.

# Returns

```
PPL_PIP_PROBLEM_STATUS_UNFEASIBLE if the PIP problem is not satisfiable; PPL_PIP_-
PROBLEM_STATUS_OPTIMIZED if the PIP problem admits an optimal solution.
```

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.20 ppl\_PIP\_Solution\_Node\_tag Interface Reference

Types and functions for PIP solution nodes.

#include <ppl\_c\_header.h>

# **Related Functions**

(Note that these are not member functions.)

int ppl\_PIP\_Solution\_Node\_get\_parametric\_values (ppl\_const\_PIP\_Solution\_Node\_t pip\_sol, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t \*le)

Writes to le a const pointer to the parametric expression of the values of variable var in solution node pip\_sol.

## **Input/Output Functions**

- int ppl\_io\_print\_PIP\_Solution\_Node (ppl\_const\_PIP\_Solution\_Node\_t x) *Prints x to stdout*.
- int ppl\_io\_fprint\_PIP\_Solution\_Node (FILE \*stream, ppl\_const\_PIP\_Solution\_Node\_t x) Prints x to the given output stream.
- int ppl\_io\_asprint\_PIP\_Solution\_Node (char \*\*strp, ppl\_const\_PIP\_Solution\_Node\_t x) Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_PIP\_Solution\_Node\_ascii\_dump (ppl\_const\_PIP\_Solution\_Node\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_PIP\_Solution\_Node\_ascii\_load (ppl\_PIP\_Solution\_Node\_t x, FILE \*stream) Loads an ascii representation of x from stream.

### 7.20.1 Detailed Description

Types and functions for PIP solution nodes. The types and functions for solution nodes provide an interface towards *PIP\_Solution\_Node*.

# 7.20.2 Friends And Related Function Documentation

Writes to le a const pointer to the parametric expression of the values of variable var in solution node pip\_sol.

The linear expression assigned to le will only refer to (problem or artificial) parameters.

# Parameters

pip\_sol The solution tree node.

var The variable which is queried about.

*le* The returned expression for variable var.

# Returns

**PPL\_ERROR\_INVALID\_ARGUMENT** Returned if var is dimension-incompatible with \*this or if var is a problem parameter.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.21 ppl\_PIP\_Tree\_Node\_tag Interface Reference

Types and functions for generic PIP tree nodes.

#include <ppl\_c\_header.h>

# **Related Functions**

(Note that these are not member functions.)

• int ppl\_PIP\_Tree\_Node\_as\_solution (ppl\_const\_PIP\_Tree\_Node\_t spip\_tree, ppl\_const\_PIP\_Solution\_Node\_t \*dpip\_tree)

Writes to dpip\_tree the solution node if spip\_tree is a solution node, and 0 otherwise.

int ppl\_PIP\_Tree\_Node\_as\_decision (ppl\_const\_PIP\_Tree\_Node\_t spip\_tree, ppl\_const\_PIP\_Decision\_Node\_t \*dpip\_tree)

Writes to dpip\_tree the decision node if spip\_tree is a decision node, and 0 otherwise.

• int ppl\_PIP\_Tree\_Node\_get\_constraints (ppl\_const\_PIP\_Tree\_Node\_t pip\_tree, ppl\_const\_Constraint\_System\_t \*pcs)

Writes to pcs the local system of parameter constraints at the pip tree node pip\_tree.

• int ppl\_PIP\_Tree\_Node\_OK (ppl\_const\_PIP\_Tree\_Node\_t pip)

Returns a positive integer if pip\_tree is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if pip\_tree is broken. Useful for debugging purposes.

• int ppl\_PIP\_Tree\_Node\_number\_of\_artificials (ppl\_const\_PIP\_Tree\_Node\_t pip\_tree, ppl\_dimension\_type \*m)

Writes to m the number of elements in the artificial parameter sequence in the pip tree node pip\_tree.

• int ppl\_PIP\_Tree\_Node\_begin (ppl\_const\_PIP\_Tree\_Node\_t pip\_tree, ppl\_Artificial\_Parameter\_-Sequence\_const\_iterator\_t pit)

Assigns to pit a const iterator "pointing" to the beginning of the artificial parameter sequence in the pip tree node pip\_tree.

• int ppl\_PIP\_Tree\_Node\_end (ppl\_const\_PIP\_Tree\_Node\_t pip\_tree, ppl\_Artificial\_Parameter\_-Sequence\_const\_iterator\_t pit)

Assigns to pit a const iterator "pointing" to the end of the artificial parameter sequence in the pip tree node pip\_tree.

# **Input/Output Functions**

- int ppl\_io\_print\_PIP\_Tree\_Node (ppl\_const\_PIP\_Tree\_Node\_t x)
   Prints x to stdout.
- int ppl\_io\_fprint\_PIP\_Tree\_Node (FILE \*stream, ppl\_const\_PIP\_Tree\_Node\_t x)
   Prints x to the given output stream.
- int ppl\_io\_asprint\_PIP\_Tree\_Node (char \*\*strp, ppl\_const\_PIP\_Tree\_Node\_t x) Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_PIP\_Tree\_Node\_ascii\_dump (ppl\_const\_PIP\_Tree\_Node\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_PIP\_Tree\_Node\_ascii\_load (ppl\_PIP\_Tree\_Node\_t x, FILE \*stream) Loads an ascii representation of x from stream.

# 7.21.1 Detailed Description

Types and functions for generic PIP tree nodes. The types and functions for tree nodes provide an interface towards *PIP\_Tree\_Node*.

The documentation for this interface was generated from the following file:

• ppl\_c\_header.h

# 7.22 ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_tag Interface Reference

Types and functions for iterating on the disjuncts of a const ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag.

# **Related Functions**

(Note that these are not member functions.)

#### **Construction, Initialization and Destruction**

 int ppl\_new\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_const\_iterator\_t \*pit)

Builds a new 'const iterator' and writes a handle to it at address pit.

- int ppl\_new\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_from\_const\_iterator (ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t \*pit, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t y)
  - Builds a copy of y and writes a handle to it at address pit.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_begin (ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_t ps, ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t psit) Assigns to psit a const iterator "pointing" to the beginning of the sequence of disjuncts of ps.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_end (ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_t ps, ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t psit) Assigns to psit a const iterator "pointing" past the end of the sequence of disjuncts of ps.
- int ppl\_delete\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator (ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_const\_iterator\_t it)

Invalidates the handle it: this makes sure the corresponding resources will eventually be released.

## Dereferencing, Increment, Decrement and Equality Testing

- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_dereference (ppl\_const\_Pointset\_-Powerset\_C\_Polyhedron\_const\_iterator\_t it, ppl\_const\_Polyhedron\_t \*d) Dereferences it writing a const handle to the resulting disjunct at address d.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_increment (ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t it)
   Increments it so that it "points" to the next disjunct.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_decrement (ppl\_Pointset\_Powerset\_-C\_Polyhedron\_const\_iterator\_t it)

Decrements it so that it "points" to the previous disjunct.

int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_equal\_test (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t x, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t y)

Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

#### 7.22.1 Detailed Description

Types and functions for iterating on the disjuncts of a const ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag.

# 7.22.2 Friends And Related Function Documentation

7.22.2.1 int ppl\_Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_dereference (ppl\_const\_-Pointset\_Powerset\_C\_Polyhedron\_const\_iterator\_t *it*, ppl\_const\_Polyhedron\_t \* *d*) [related]

Dereferences it writing a const handle to the resulting disjunct at address d.

## Warning

On exit, the disjunct d is still owned by the powerset object: any function call on the owning powerset object may invalidate it. Moreover, d should **not** be deleted directly: its resources will be released when deleting the owning powerset.

The documentation for this interface was generated from the following file:

• C\_interface.dox

# 7.23 ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_tag Interface Reference

Types and functions for iterating on the disjuncts of a ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag.

# **Related Functions**

(Note that these are not member functions.)

#### **Construction, Initialization and Destruction**

- int ppl\_new\_Pointset\_Powerset\_C\_Polyhedron\_iterator (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_iterator\_t \*pit) Builds a new 'iterator' and writes a handle to it at address pit.
- int ppl\_new\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_from\_iterator (ppl\_Pointset\_Powerset\_-C\_Polyhedron\_iterator\_t \*pit, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t y) Builds a copy of y and writes a handle to it at address pit.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_begin (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_t ps, ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t psit) Assigns to psit an iterator "pointing" to the beginning of the sequence of disjuncts of ps.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_end (ppl\_Pointset\_Powerset\_C\_Polyhedron\_t ps, ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t psit)
   Assigns to psit an iterator "pointing" past the end of the sequence of disjuncts of ps.
- int ppl\_delete\_Pointset\_Powerset\_C\_Polyhedron\_iterator (ppl\_const\_Pointset\_Powerset\_C\_-Polyhedron\_iterator\_t it)

# Dereferencing, Increment, Decrement and Equality Testing

Invalidates the handle it: this makes sure the corresponding resources will eventually be released.

- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_dereference (ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_iterator\_t it, ppl\_const\_Polyhedron\_t \*d)
   Dereferences it writing a const handle to the resulting disjunct at address d.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_increment (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_iterator\_t it)

Increments it so that it "points" to the next disjunct.

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_decrement (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_iterator\_t it)

Decrements it so that it "points" to the previous disjunct.

- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_equal\_test (ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_iterator\_t x, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t y)
  - Returns a positive integer if the iterators corresponding to x and y are equal; returns 0 if they are different.

#### 7.23.1 Detailed Description

Types and functions for iterating on the disjuncts of a ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag.

#### 7.23.2 Friends And Related Function Documentation

#### 7.23.2.1 int ppl\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_dereference (ppl\_const\_-Pointset\_Powerset\_C\_Polyhedron\_iterator\_t *it*, ppl\_const\_Polyhedron\_t \* *d*) [related]

Dereferences it writing a const handle to the resulting disjunct at address d.

#### Note

Even though it is an non-const iterator, dereferencing it results in a handle to a **const** disjunct. This is because mutable iterators are meant to allow for the modification of the sequence of disjuncts (e.g., by dropping elements), while preventing direct modifications of the disjuncts they point to.

#### Warning

On exit, the disjunct d is still owned by the powerset object: any function call on the owning powerset object may invalidate it. Moreover, d should **not** be deleted directly: its resources will be released when deleting the owning powerset.

The documentation for this interface was generated from the following file:

• C\_interface.dox

#### 7.24 ppl\_Pointset\_Powerset\_C\_Polyhedron\_tag Interface Reference

Types and functions for the Pointset\_Powerset of C\_Polyhedron objects.

#### **Related Functions**

(Note that these are not member functions.)

#### Ad Hoc Functions for Pointset\_Powerset domains

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_omega\_reduce (ppl\_const\_Pointset\_Powerset\_C\_-Polyhedron\_t ps)

Drops from the sequence of disjuncts in ps all the non-maximal elements so that ps is non-redundant.

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_size (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_t ps, size\_t \*sz)

Writes to sz the number of disjuncts in ps.

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_geometrically\_covers\_Pointset\_Powerset\_C\_-Polyhedron (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_t x, ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_t y)

Returns a positive integer if powerset x geometrically covers powerset y; returns 0 otherwise.

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_geometrically\_equals\_Pointset\_Powerset\_C\_-Polyhedron (ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_t x, ppl\_const\_Pointset\_Powerset\_-C\_Polyhedron\_t y)

Returns a positive integer if powerset x is geometrically equal to powerset y; returns 0 otherwise.

- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_add\_disjunct (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_t ps, ppl\_const\_Polyhedron\_t d) Adds to ps a copy of disjunct d.
- int ppl\_Pointset\_Powerset\_C\_Polyhedron\_drop\_disjunct (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_t ps, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t cit, ppl\_Pointset\_-Powerset\_C\_Polyhedron\_iterator\_t it)

Drops from ps the disjunct pointed to by cit, assigning to it an iterator to the disjunct following cit.

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_drop\_disjuncts (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_t ps, ppl\_const\_Pointset\_Powerset\_C\_Polyhedron\_iterator\_t first, ppl\_const\_-Pointset\_Powerset\_C\_Polyhedron\_iterator\_t last)

Drops from ps all the disjuncts from first to last (excluded).

• int ppl\_Pointset\_Powerset\_C\_Polyhedron\_pairwise\_reduce (ppl\_Pointset\_Powerset\_C\_-Polyhedron\_t ps)

Modifies ps by (recursively) merging together the pairs of disjuncts whose upper-bound is the same as their set-theoretical union.

#### 7.24.1 Detailed Description

Types and functions for the Pointset\_Powerset of C\_Polyhedron objects. The powerset domains can be instantiated by taking as a base domain any fixed semantic geometric description (C and NNC polyhedra, BD and octagonal shapes, boxes and grids). An element of the powerset domain represents a disjunctive collection of base objects (its disjuncts), all having the same space dimension.

Besides the functions that are available in all semantic geometric descriptions (whose documentation is not repeated here), the powerset domain also provides several ad hoc functions. In particular, the iterator types allow for the examination and manipulation of the collection of disjuncts.

#### 7.24.2 Friends And Related Function Documentation

7.24.2.1 int ppl\_Pointset\_Powerset\_C\_Polyhedron\_size (ppl\_const\_Pointset\_Powerset\_C\_-Polyhedron\_t ps, size\_t \* sz) [related]

Writes to sz the number of disjuncts in ps.

#### Note

If present, Omega-redundant elements will be counted too.

The documentation for this interface was generated from the following file:

• C\_interface.dox

#### 7.25 ppl\_Polyhedron\_tag Interface Reference

Types and functions for the domains of C and NNC convex polyhedra.

#### **Related Functions**

(Note that these are not member functions.)

#### Constructors and Assignment for C\_Polyhedron

• int ppl\_new\_C\_Polyhedron\_from\_space\_dimension (ppl\_Polyhedron\_t \*pph, ppl\_dimension\_type d, int empty)

Builds a C polyhedron of dimension d and writes an handle to it at address pph. If empty is different from zero, the newly created polyhedron will be empty; otherwise, it will be a universe polyhedron.

• int ppl\_new\_C\_Polyhedron\_from\_C\_Polyhedron (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph)

Builds a C polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_C\_Polyhedron\_from\_C\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph, int complexity)

Builds a C polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_C\_Polyhedron\_from\_Constraint\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Constraint\_System\_t cs)

Builds a new C polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_C\_Polyhedron\_recycle\_Constraint\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Constraint\_System\_t cs)

Builds a new C polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_C\_Polyhedron\_from\_Congruence\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Congruence\_System\_t cs) Builds a new C polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_C\_Polyhedron\_recycle\_Congruence\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Congruence\_System\_t cs)

Builds a new C polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_assign\_C\_Polyhedron\_from\_C\_Polyhedron (ppl\_Polyhedron\_t dst, ppl\_const\_Polyhedron\_t src)

Assigns a copy of the C polyhedron src to the C polyhedron dst.

#### Constructors and Assignment for NNC\_Polyhedron

 int ppl\_new\_NNC\_Polyhedron\_from\_space\_dimension (ppl\_Polyhedron\_t \*pph, ppl\_dimension\_type d, int empty)

Builds an NNC polyhedron of dimension d and writes an handle to it at address pph. If empty is different from zero, the newly created polyhedron will be empty; otherwise, it will be a universe polyhedron.

 int ppl\_new\_NNC\_Polyhedron\_from\_NNC\_Polyhedron (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Polyhedron\_t ph)

Builds an NNC polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_from\_NNC\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph, int complexity)

Builds an NNC polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_from\_Constraint\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_ Constraint\_System\_t cs)

Builds a new NNC polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_recycle\_Constraint\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Constraint\_System\_t cs)

Builds a new NNC polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_from\_Congruence\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Congruence\_System\_t cs)

Builds a new NNC polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_recycle\_Congruence\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Congruence\_System\_t cs)

Builds a new NNC polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_assign\_NNC\_Polyhedron\_from\_NNC\_Polyhedron (ppl\_Polyhedron\_t dst, ppl\_const\_Polyhedron\_t src)

Assigns a copy of the NNC polyhedron src to the NNC polyhedron dst.

#### **Constructors Behaving as Conversion Operators**

Besides the conversions listed here below, the library also provides conversion operators that build a semantic geometric description starting from **any** other semantic geometric description (e.g., ppl\_new\_Grid\_from\_C\_Polyhedron, ppl\_new\_C\_Polyhedron\_from\_BD\_Shape\_mpq\_class, etc.). Clearly, the conversion operators are only available if both the source and the target semantic geometric descriptions have been enabled when configuring the library. The conversions also taking as argument a complexity class sometimes provide non-trivial precision/efficiency trade-offs.

• int ppl\_new\_C\_Polyhedron\_from\_NNC\_Polyhedron (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph)

Builds a C polyhedron that is a copy of the topological closure of the NNC polyhedron ph; writes a handle for the newly created polyhedron at address pph.

 int ppl\_new\_C\_Polyhedron\_from\_NNC\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph, int complexity)

Builds a C polyhedron that approximates NNC\_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_from\_C\_Polyhedron (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph)

Builds an NNC polyhedron that is a copy of the C polyhedron ph; writes a handle for the newly created polyhedron at address pph.

 int ppl\_new\_NNC\_Polyhedron\_from\_C\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \*pph, ppl\_const\_Polyhedron\_t ph, int complexity)

Builds an NNC polyhedron that approximates C\_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

#### Destructor for (C or NNC) Polyhedra

• int ppl\_delete\_Polyhedron (ppl\_const\_Polyhedron\_t ph) Invalidates the handle ph: this makes sure the corresponding resources will eventually be released.

#### Functions that Do Not Modify the Polyhedron

- int ppl\_Polyhedron\_space\_dimension (ppl\_const\_Polyhedron\_t ph, ppl\_dimension\_type \*m) Writes to m the dimension of the vector space enclosing ph.
- int ppl\_Polyhedron\_affine\_dimension (ppl\_const\_Polyhedron\_t ph, ppl\_dimension\_type \*m) Writes to m the affine dimension of ph (not to be confused with the dimension of its enclosing vector space) or 0, if ph is empty.
- int ppl\_Polyhedron\_relation\_with\_Constraint (ppl\_const\_Polyhedron\_t ph, ppl\_const\_-Constraint\_t c)

*Checks the relation between the polyhedron* ph and the constraint c.

• int ppl\_Polyhedron\_relation\_with\_Generator (ppl\_const\_Polyhedron\_t ph, ppl\_const\_-Generator\_t g)

 $Checks \ the \ relation \ between \ the \ polyhedron \ ph \ and \ the \ generator \ g.$ 

 int ppl\_Polyhedron\_get\_constraints (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Constraint\_-System\_t \*pcs) Writes a const handle to the constraint system defining the polyhedron ph at address pcs.

 int ppl\_Polyhedron\_get\_congruences (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Congruence\_-System\_t \*pcs)

Writes at address pcs a const handle to a system of congruences approximating the polyhedron ph.

• int ppl\_Polyhedron\_get\_minimized\_constraints (ppl\_const\_Polyhedron\_t ph, ppl\_const\_ Constraint\_System\_t \*pcs)

Writes a const handle to the minimized constraint system defining the polyhedron ph at address pcs.

int ppl\_Polyhedron\_get\_minimized\_congruences (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Congruence\_System\_t \*pcs)

Writes at address pcs a const handle to a system of minimized congruences approximating the polyhedron ph.

- int ppl\_Polyhedron\_is\_empty (ppl\_const\_Polyhedron\_t ph) Returns a positive integer if ph is empty; returns 0 if ph is not empty.
- int ppl\_Polyhedron\_is\_universe (ppl\_const\_Polyhedron\_t ph) Returns a positive integer if ph is a universe polyhedron; returns 0 if it is not.
- int ppl\_Polyhedron\_is\_bounded (ppl\_const\_Polyhedron\_t ph) Returns a positive integer if ph is bounded; returns 0 if ph is unbounded.
- int ppl\_Polyhedron\_contains\_integer\_point (ppl\_const\_Polyhedron\_t ph) Returns a positive integer if ph contains at least one integer point; returns 0 otherwise.
- int ppl\_Polyhedron\_is\_topologically\_closed (ppl\_const\_Polyhedron\_t ph) Returns a positive integer if ph is topologically closed; returns 0 if ph is not topologically closed.
- int ppl\_Polyhedron\_is\_discrete (ppl\_const\_Polyhedron\_t ph) Returns a positive integer if ph is a discrete set; returns 0 if ph is not a discrete set.
- int ppl\_Polyhedron\_constrains (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var) Returns a positive integer if ph constrains var; returns 0 if ph does not constrain var.
- int ppl\_Polyhedron\_bounds\_from\_above (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_-Expression\_t le)

Returns a positive integer if le is bounded from above in ph; returns 0 otherwise.

• int ppl\_Polyhedron\_bounds\_from\_below (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_-Expression\_t le)

Returns a positive integer if le is bounded from below in ph; returns 0 otherwise.

• int ppl\_Polyhedron\_maximize\_with\_point (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_ Expression\_t le, ppl\_Coefficient\_t sup\_n, ppl\_Coefficient\_t sup\_d, int \*pmaximum, ppl\_-Generator\_t point)

Returns a positive integer if ph is not empty and le is bounded from above in ph, in which case the supremum value and a point where le reaches it are computed.

• int ppl\_Polyhedron\_maximize (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_Expression\_t le, ppl\_Coefficient\_t sup\_n, ppl\_Coefficient\_t sup\_d, int \*pmaximum)

The same as ppl\_Polyhedron\_maximize\_with\_point, but without the output argument for the location where the supremum value is reached.

• int ppl\_Polyhedron\_minimize\_with\_point (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_ Expression\_t le, ppl\_Coefficient\_t inf\_n, ppl\_Coefficient\_t inf\_d, int \*pminimum, ppl\_-Generator\_t point)

Returns a positive integer if ph is not empty and le is bounded from below in ph, in which case the infimum value and a point where le reaches it are computed.

 int ppl\_Polyhedron\_minimize\_with\_point (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_-Expression\_t le, ppl\_Coefficient\_t inf\_n, ppl\_Coefficient\_t inf\_d, int \*pminimum)

The same as ppl\_Polyhedron\_minimize\_with\_point, but without the output argument for the location where the infimum value is reached.

• int ppl\_Polyhedron\_contains\_Polyhedron (ppl\_const\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

Returns a positive integer if x contains or is equal to y; returns 0 if it does not.

• int ppl\_Polyhedron\_strictly\_contains\_Polyhedron (ppl\_const\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

Returns a positive integer if x strictly contains y; returns 0 if it does not.

int ppl\_Polyhedron\_is\_disjoint\_from\_Polyhedron (ppl\_const\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

Returns a positive integer if x and y are disjoint; returns 0 if they are not.

- int ppl\_Polyhedron\_equals\_Polyhedron (ppl\_const\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) *Returns a positive integer if x and y are the same polyhedron; returns 0 if they are different.*
- int ppl\_Polyhedron\_OK (ppl\_const\_Polyhedron\_t ph) *Returns a positive integer if ph is well formed, i.e., if it satisfies all its implementation invariants; returns 0 and perhaps makes some noise if ph is broken. Useful for debugging purposes.*
- int ppl\_Polyhedron\_external\_memory\_in\_bytes (ppl\_const\_Polyhedron\_t ph, size\_t \*sz) Writes to sz a lower bound to the size in bytes of the memory managed by ph.
- int ppl\_Polyhedron\_total\_memory\_in\_bytes (ppl\_const\_Polyhedron\_t ph, size\_t \*sz) Writes to sz a lower bound to the size in bytes of the memory managed by ph.

#### Space Dimension Preserving Functions that May Modify the Polyhedron

- int ppl\_Polyhedron\_add\_constraint (ppl\_Polyhedron\_t ph, ppl\_const\_Constraint\_t c) Adds a copy of the constraint c to the system of constraints of ph.
- int ppl\_Polyhedron\_add\_congruence (ppl\_Polyhedron\_t ph, ppl\_const\_Congruence\_t c) Adds a copy of the congruence c to polyhedron of ph.
- int ppl\_Polyhedron\_add\_constraints (ppl\_Polyhedron\_t ph, ppl\_const\_Constraint\_System\_t cs) Adds a copy of the system of constraints cs to the system of constraints of ph.
- int ppl\_Polyhedron\_add\_congruences (ppl\_Polyhedron\_t ph, ppl\_const\_Congruence\_System\_t cs)

Adds a copy of the system of congruences cs to the polyhedron ph.

• int ppl\_Polyhedron\_add\_recycled\_constraints (ppl\_Polyhedron\_t ph, ppl\_Constraint\_System\_t cs)

Adds the system of constraints cs to the system of constraints of ph.

• int ppl\_Polyhedron\_add\_recycled\_congruences (ppl\_Polyhedron\_t ph, ppl\_Congruence\_-System\_t cs)

Adds the system of congruences cs to the polyhedron ph.

- int ppl\_Polyhedron\_refine\_with\_constraint (ppl\_Polyhedron\_t ph, ppl\_const\_Constraint\_t c) *Refines* ph using constraint c.
- int ppl\_Polyhedron\_refine\_with\_congruence (ppl\_Polyhedron\_t ph, ppl\_const\_Congruence\_t c) *Refines* ph using congruence c.
- int ppl\_Polyhedron\_refine\_with\_constraints (ppl\_Polyhedron\_t ph, ppl\_const\_Constraint\_-System\_t cs)

Refines ph using the constraints in cs.

• int ppl\_Polyhedron\_refine\_with\_congruences (ppl\_Polyhedron\_t ph, ppl\_const\_Congruence\_-System\_t cs)

Refines ph using the congruences in cs.

- int ppl\_Polyhedron\_intersection\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) Intersects x with polyhedron y and assigns the result to x.
- int ppl\_Polyhedron\_upper\_bound\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) Assigns to x an upper bound of x and y.
- int ppl\_Polyhedron\_difference\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) Same as ppl\_Polyhedron\_poly\_difference\_assign(x, y).
- int ppl\_Polyhedron\_simplify\_using\_context\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

Assigns to x the meet-preserving simplification of x with respect to context y. Returns a positive integer if x and y have a nonempty intersection; returns 0 if they are disjoint.

- int ppl\_Polyhedron\_time\_elapse\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) Assigns to x the time-elapse between the polyhedra x and y.
- int ppl\_Polyhedron\_topological\_closure\_assign (ppl\_Polyhedron\_t ph) Assigns to ph its topological closure.
- int ppl\_Polyhedron\_unconstrain\_space\_dimension (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var)

Modifies ph by unconstraining the space dimension var.

• int ppl\_Polyhedron\_unconstrain\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type ds[], size\_t n)

Modifies ph by unconstraining the space dimensions that are specified in the first n positions of the array ds. The presence of duplicates in ds is a waste but an innocuous one.

 int ppl\_Polyhedron\_affine\_image (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_ Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d)

Transforms the polyhedron ph, assigning an affine expression to the specified variable.

- int ppl\_Polyhedron\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d)
   Transforms the polyhedron ph, substituting an affine expression to the specified variable.
- int ppl\_Polyhedron\_bounded\_affine\_image (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t lb, ppl\_const\_Linear\_Expression\_t ub, ppl\_const\_Coefficient\_t d)
   Assigns to ph the image of ph with respect to the generalized affine transfer relation <sup>lb</sup>/<sub>d</sub> ≤ var' ≤ <sup>ub</sup>/<sub>d</sub>.
- int ppl\_Polyhedron\_bounded\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t lb, ppl\_const\_Linear\_Expression\_t ub, ppl\_const\_Coefficient\_t d)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation  $\frac{lb}{d} \leq var' \leq \frac{ub}{d}$ .

• int ppl\_Polyhedron\_generalized\_affine\_image (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_-Coefficient\_t d)

Assigns to ph the image of ph with respect to the generalized affine transfer relation  $\operatorname{var}' \bowtie \frac{\operatorname{le}}{\operatorname{d}}$ , where  $\bowtie$  is the relation symbol encoded by relsym.

• int ppl\_Polyhedron\_generalized\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation  $var' \bowtie \frac{le}{d}$ , where  $\bowtie$  is the relation symbol encoded by relsym.

 int ppl\_Polyhedron\_generalized\_affine\_image\_lhs\_rhs (ppl\_Polyhedron\_t ph, ppl\_const\_ Linear\_Expression\_t lhs, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_ Expression\_t rhs)

Assigns to ph the image of ph with respect to the generalized affine transfer relation  $lhs' \bowtie rhs$ , where  $\bowtie$  is the relation symbol encoded by relsym.

 int ppl\_Polyhedron\_generalized\_affine\_preimage\_lhs\_rhs (ppl\_Polyhedron\_t ph, ppl\_const\_ Linear\_Expression\_t lhs, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_ Expression\_t rhs)

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation  $lhs' \bowtie rhs$ , where  $\bowtie$  is the relation symbol encoded by relsym.

#### Functions that May Modify the Dimension of the Vector Space

• int ppl\_Polyhedron\_concatenate\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

Seeing a polyhedron as a set of tuples (its points), assigns to x all the tuples that can be obtained by concatenating, in the order given, a tuple of x with a tuple of y.

• int ppl\_Polyhedron\_add\_space\_dimensions\_and\_embed (ppl\_Polyhedron\_t ph, ppl\_dimension\_type d)

Adds d new dimensions to the space enclosing the polyhedron ph and to ph itself.

 int ppl\_Polyhedron\_add\_space\_dimensions\_and\_project (ppl\_Polyhedron\_t ph, ppl\_dimension\_type d)

Adds d new dimensions to the space enclosing the polyhedron ph.

• int ppl\_Polyhedron\_remove\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type ds[], size\_t n)

Removes from the vector space enclosing ph the space dimensions that are specified in first n positions of the array ds. The presence of duplicates in ds is a waste but an innocuous one.

 int ppl\_Polyhedron\_remove\_higher\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type d)

*Removes the higher dimensions from the vector space enclosing* ph *so that, upon successful return, the new space dimension is* d.

int ppl\_Polyhedron\_map\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type maps[], size\_t n)

*Remaps the dimensions of the vector space according to a partial function. This function is specified by means of the maps array, which has n entries.* 

• int ppl\_Polyhedron\_expand\_space\_dimension (ppl\_Polyhedron\_t ph, ppl\_dimension\_type d, ppl\_dimension\_type m)

Expands the d-th dimension of the vector space enclosing ph to m new space dimensions.

• int ppl\_Polyhedron\_fold\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type ds[], size\_t n, ppl\_dimension\_type d)

Modifies ph by folding the space dimensions contained in the first n positions of the array ds into dimension d. The presence of duplicates in ds is a waste but an innocuous one.

#### **Input/Output Functions**

- int ppl\_io\_print\_Polyhedron (ppl\_const\_Polyhedron\_t x)
   Prints x to stdout.
- int ppl\_io\_fprint\_Polyhedron (FILE \*stream, ppl\_const\_Polyhedron\_t x)
   Prints x to the given output stream.
- int ppl\_io\_asprint\_Polyhedron (char \*\*strp, ppl\_const\_Polyhedron\_t x)
   Prints x to a malloc-allocated string, a pointer to which is returned via strp.
- int ppl\_Polyhedron\_ascii\_dump (ppl\_const\_Polyhedron\_t x, FILE \*stream) Dumps an ascii representation of x on stream.
- int ppl\_Polyhedron\_ascii\_load (ppl\_Polyhedron\_t x, FILE \*stream) Loads an ascii representation of x from stream.

#### Ad Hoc Functions for (C or NNC) Polyhedra

The functions listed here below, being specific of the polyhedron domains, do not have a correspondence in other semantic geometric descriptions.

• int ppl\_new\_C\_Polyhedron\_from\_Generator\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Generator\_System\_t gs)

Builds a new C polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_C\_Polyhedron\_recycle\_Generator\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Generator\_System\_t gs)

Builds a new C polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_from\_Generator\_System (ppl\_Polyhedron\_t \*pph, ppl\_const\_-Generator\_System\_t gs)

Builds a new NNC polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_new\_NNC\_Polyhedron\_recycle\_Generator\_System (ppl\_Polyhedron\_t \*pph, ppl\_-Generator\_System\_t gs)

Builds a new NNC polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

• int ppl\_Polyhedron\_get\_generators (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Generator\_System\_t \*pgs)

Writes a const handle to the generator system defining the polyhedron ph at address pgs.

• int ppl\_Polyhedron\_get\_minimized\_generators (ppl\_const\_Polyhedron\_t ph, ppl\_const\_-Generator\_System\_t \*pgs)

Writes a const handle to the minimized generator system defining the polyhedron ph at address pgs.

- int ppl\_Polyhedron\_add\_generator (ppl\_Polyhedron\_t ph, ppl\_const\_Generator\_t g) Adds a copy of the generator g to the system of generators of ph.
- int ppl\_Polyhedron\_add\_generators (ppl\_Polyhedron\_t ph, ppl\_const\_Generator\_System\_t gs) Adds a copy of the system of generators gs to the system of generators of ph.
- int ppl\_Polyhedron\_add\_recycled\_generators (ppl\_Polyhedron\_t ph, ppl\_Generator\_System\_t gs)

Adds the system of generators gs to the system of generators of ph.

- int ppl\_Polyhedron\_poly\_hull\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) Assigns to x the poly-hull of x and y.
- int ppl\_Polyhedron\_poly\_difference\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) Assigns to x the poly-difference of x and y.
- int wrap\_assign (ppl\_Polyhedron\_t ph, ppl\_dimension\_type ds[], size\_t n, ppl\_enum\_-Bounded\_Integer\_Type\_Width w, ppl\_enum\_Bounded\_Integer\_Type\_Representation r, ppl\_ enum\_Bounded\_Integer\_Type\_Overflow o, const ppl\_const\_Constraint\_System\_t \*pcs, unsigned complexity\_threshold, int wrap\_individually)

Assigns to ph the polyhedron obtained from ph by "wrapping" the vector space defined by the first n space dimensions in ds[].

 int ppl\_Polyhedron\_BHRZ03\_widening\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_-Polyhedron\_t y, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y. If tp is not the null pointer, the widening with tokens delay technique is applied with \*tp available tokens.

• int ppl\_Polyhedron\_H79\_widening\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y. If tp is not the null pointer, the widening with tokens delay technique is applied with \*tp available tokens.

• int ppl\_Polyhedron\_BHRZ03\_widening\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y.

- int ppl\_Polyhedron\_H79\_widening\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y.
- int ppl\_Polyhedron\_limited\_BHRZ03\_extrapolation\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with tp available tokens.

• int ppl\_Polyhedron\_limited\_H79\_extrapolation\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with tp available tokens.

• int ppl\_Polyhedron\_limited\_BHRZ03\_extrapolation\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x.

• int ppl\_Polyhedron\_limited\_H79\_extrapolation\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x.

• int ppl\_Polyhedron\_bounded\_BHRZ03\_extrapolation\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form  $\pm v \leq r$  and  $\pm v < r$ , with  $r \in \mathbb{Q}$ , that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with  $\pm tp$  available tokens.

• int ppl\_Polyhedron\_bounded\_H79\_extrapolation\_assign\_with\_tokens (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs, unsigned \*tp)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form  $\pm v \leq r$  and  $\pm v < r$ , with  $r \in \mathbb{Q}$ , that are satisfied by all the points of x. If tp is not the null pointer, the widening with tokens delay technique is applied with tp available tokens.

• int ppl\_Polyhedron\_bounded\_BHRZ03\_extrapolation\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the BHRZ03-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form  $\pm v \leq r$  and  $\pm v < r$ , with  $r \in \mathbb{Q}$ , that are satisfied by all the points of x.

• int ppl\_Polyhedron\_bounded\_H79\_extrapolation\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y, ppl\_const\_Constraint\_System\_t cs)

If the polyhedron y is contained in (or equal to) the polyhedron x, assigns to x the H79-widening of x and y intersected with the constraints in cs that are satisfied by all the points of x, further intersected with all the constraints of the form  $\pm v \leq r$  and  $\pm v < r$ , with  $r \in \mathbb{Q}$ , that are satisfied by all the points of x.

#### 7.25.1 Detailed Description

Types and functions for the domains of C and NNC convex polyhedra. The types and functions for convex polyhedra provide a single interface for accessing both topologically closed (C) and not necessarily closed (NNC) convex polyhedra. The distinction between C and NNC polyhedra need only be explicitly stated when *creating* or *assigning* a polyhedron object, by means of one of the functions ppl\_new\_\* and ppl\_-assign\_\*.

Having a single datatype does not mean that C and NNC polyhedra can be freely interchanged: as specified in the main manual, most library functions require their arguments to be topologically and/or spacedimension compatible.

#### 7.25.2 Friends And Related Function Documentation

## 7.25.2.1 int ppl\_new\_C\_Polyhedron\_from\_C\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \* *pph*, ppl\_const\_Polyhedron\_t *ph*, int *complexity*) [related]

Builds a C polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

#### Note

The complexity argument is ignored.

# 7.25.2.2 int ppl\_new\_C\_Polyhedron\_from\_Constraint\_System (ppl\_Polyhedron\_t \* *pph*, ppl\_const\_Constraint\_System\_t *cs*) [related]

Builds a new C polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

## 7.25.2.3 int ppl\_new\_C\_Polyhedron\_recycle\_Constraint\_System (ppl\_Polyhedron\_t \* *pph*, ppl\_Constraint\_System\_t *cs*) [related]

Builds a new C polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

#### Warning

This function modifies the constraint system referenced by cs: upon return, no assumption can be made on its value.

## 7.25.2.4 int ppl\_new\_C\_Polyhedron\_from\_Congruence\_System (ppl\_Polyhedron\_t \* *pph*, ppl\_const\_Congruence\_System\_t *cs*) [related]

Builds a new C polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

# 7.25.2.5 int ppl\_new\_C\_Polyhedron\_recycle\_Congruence\_System (ppl\_Polyhedron\_t \* *pph*, ppl\_Congruence\_System\_t *cs*) [related]

Builds a new C polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

#### Warning

This function modifies the congruence system referenced by cs: upon return, no assumption can be made on its value.

#### 7.25.2.6 int ppl\_new\_NNC\_Polyhedron\_from\_NNC\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \* pph, ppl\_const\_Polyhedron\_t ph, int complexity) [related]

Builds an NNC polyhedron that is a copy of ph; writes a handle for the newly created polyhedron at address pph.

#### Note

The complexity argument is ignored.

# 7.25.2.7 int ppl\_new\_NNC\_Polyhedron\_from\_Constraint\_System (ppl\_Polyhedron\_t \* *pph*, ppl\_const\_Constraint\_System\_t *cs*) [related]

Builds a new NNC polyhedron from the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

# 7.25.2.8 int ppl\_new\_NNC\_Polyhedron\_recycle\_Constraint\_System (ppl\_Polyhedron\_t \* *pph*, ppl\_Constraint\_System\_t *cs*) [related]

Builds a new NNC polyhedron recycling the system of constraints cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

#### Warning

This function modifies the constraint system referenced by cs: upon return, no assumption can be made on its value.

# 7.25.2.9 int ppl\_new\_NNC\_Polyhedron\_from\_Congruence\_System (ppl\_Polyhedron\_t \* *pph*, ppl\_const\_Congruence\_System\_t *cs*) [related]

Builds a new NNC polyhedron from the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

## 7.25.2.10 int ppl\_new\_NNC\_Polyhedron\_recycle\_Congruence\_System (ppl\_Polyhedron\_t \* pph, ppl\_Congruence\_System\_t cs) [related]

Builds a new NNC polyhedron recycling the system of congruences cs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of cs.

#### Warning

This function modifies the congruence system referenced by cs: upon return, no assumption can be made on its value.

#### 7.25.2.11 int ppl\_new\_C\_Polyhedron\_from\_NNC\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \* pph, ppl\_const\_Polyhedron\_t ph, int complexity) [related]

Builds a C polyhedron that approximates NNC\_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

#### Note

The complexity argument, which can take values PPL\_COMPLEXITY\_CLASS\_POLYNOMIAL, PPL\_COMPLEXITY\_CLASS\_SIMPLEX and PPL\_COMPLEXITY\_CLASS\_ANY, is ignored since the exact constructor has polynomial complexity.

#### 7.25.2.12 int ppl\_new\_NNC\_Polyhedron\_from\_C\_Polyhedron\_with\_complexity (ppl\_Polyhedron\_t \* *pph*, ppl\_const\_Polyhedron\_t *ph*, int *complexity*) [related]

Builds an NNC polyhedron that approximates C\_Polyhedron ph, using an algorithm whose complexity does not exceed complexity; writes a handle for the newly created polyhedron at address pph.

#### Note

The complexity argument, which can take values PPL\_COMPLEXITY\_CLASS\_POLYNOMIAL, PPL\_COMPLEXITY\_CLASS\_SIMPLEX and PPL\_COMPLEXITY\_CLASS\_ANY, is ignored since the exact constructor has polynomial complexity.

# 7.25.2.13 int ppl\_Polyhedron\_relation\_with\_Constraint (ppl\_const\_Polyhedron\_t *ph*, ppl\_const\_Constraint\_t *c*) [related]

Checks the relation between the polyhedron ph and the constraint c.

If successful, returns a non-negative integer that is obtained as the bitwise or of the bits (chosen among PPL\_POLY\_CON\_RELATION\_IS\_DISJOINT PPL\_POLY\_CON\_RELATION\_STRICTLY\_-INTERSECTS, PPL\_POLY\_CON\_RELATION\_IS\_INCLUDED, and PPL\_POLY\_CON\_RELATION\_-SATURATES) that describe the relation between ph and c.

# 7.25.2.14 int ppl\_Polyhedron\_relation\_with\_Generator (ppl\_const\_Polyhedron\_t *ph*, ppl\_const\_Generator\_t *g*) [related]

Checks the relation between the polyhedron ph and the generator g.

If successful, returns a non-negative integer that is obtained as the bitwise or of the bits (only PPL\_POLY\_-GEN\_RELATION\_SUBSUMES, at present) that describe the relation between ph and g.

#### 7.25.2.15 int ppl\_Polyhedron\_maximize\_with\_point (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_Expression\_t le, ppl\_Coefficient\_t sup\_n, ppl\_Coefficient\_t sup\_d, int \* pmaximum, ppl\_Generator\_t point) [related]

Returns a positive integer if ph is not empty and le is bounded from above in ph, in which case the supremum value and a point where le reaches it are computed.

#### Parameters

*ph* The polyhedron constraining le;

*le* The linear expression to be maximized subject to ph;

*sup\_n* Will be assigned the numerator of the supremum value;

sup d Will be assigned the denominator of the supremum value;

pmaximum Will store 1 in this location if the supremum is also the maximum, will store 0 otherwise;

point Will be assigned the point or closure point where le reaches the extremum value.

If ph is empty or le is not bounded from above, 0 will be returned and sup\_n, sup\_d, \*pmaximum and point will be left untouched.

#### 7.25.2.16 int ppl\_Polyhedron\_minimize\_with\_point (ppl\_const\_Polyhedron\_t ph, ppl\_const\_Linear\_Expression\_t le, ppl\_Coefficient\_t inf\_n, ppl\_Coefficient\_t inf\_d, int \* pminimum, ppl\_Generator\_t point) [related]

Returns a positive integer if ph is not empty and le is bounded from below in ph, in which case the infimum value and a point where le reaches it are computed.

#### Parameters

*ph* The polyhedron constraining le;

*le* The linear expression to be minimized subject to ph;

*inf\_n* Will be assigned the numerator of the infimum value;

*inf\_d* Will be assigned the denominator of the infimum value;

pminimum Will store 1 in this location if the infimum is also the minimum, will store 0 otherwise;

point Will be assigned the point or closure point where le reaches the extremum value.

If ph is empty or le is not bounded from below, 0 will be returned and sup\_n, sup\_d, \*pmaximum and point will be left untouched.

### 7.25.2.17 int ppl\_Polyhedron\_equals\_Polyhedron (ppl\_const\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) [related]

Returns a positive integer if x and y are the same polyhedron; returns 0 if they are different.

Note that x and y may be topology- and/or dimension-incompatible polyhedra: in those cases, the value 0 is returned.

# 7.25.2.18 int ppl\_Polyhedron\_add\_recycled\_constraints (ppl\_Polyhedron\_t ph, ppl\_Constraint\_System\_t cs) [related]

Adds the system of constraints cs to the system of constraints of ph.

#### Warning

This function modifies the constraint system referenced by cs: upon return, no assumption can be made on its value.

# 7.25.2.19 int ppl\_Polyhedron\_add\_recycled\_congruences (ppl\_Polyhedron\_t ph, ppl\_Congruence\_System\_t cs) [related]

Adds the system of congruences cs to the polyhedron ph.

#### Warning

This function modifies the congruence system referenced by cs: upon return, no assumption can be made on its value.

### 7.25.2.20 int ppl\_Polyhedron\_upper\_bound\_assign (ppl\_Polyhedron\_t x, ppl\_const\_Polyhedron\_t y) [related]

Assigns to x an upper bound of x and y.

For the domain of polyhedra, this is the same as ppl\_Polyhedron\_poly\_hull\_assign(x, y).

# 7.25.2.21 int ppl\_Polyhedron\_affine\_image (ppl\_Polyhedron\_t *ph*, ppl\_dimension\_type *var*, ppl\_const\_Linear\_Expression\_t *le*, ppl\_const\_Coefficient\_t *d*) [related]

Transforms the polyhedron ph, assigning an affine expression to the specified variable.

#### Parameters

- *ph* The polyhedron that is transformed;
- var The variable to which the affine expression is assigned;
- *le* The numerator of the affine expression;
- *d* The denominator of the affine expression.

# 7.25.2.22 int ppl\_Polyhedron\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d) [related]

Transforms the polyhedron ph, substituting an affine expression to the specified variable.

#### **Parameters**

- *ph* The polyhedron that is transformed;
- *var* The variable to which the affine expression is substituted;
- *le* The numerator of the affine expression;
- *d* The denominator of the affine expression.

# 7.25.2.23 int ppl\_Polyhedron\_bounded\_affine\_image (ppl\_Polyhedron\_t *ph*, ppl\_dimension\_type *var*, ppl\_const\_Linear\_Expression\_t *lb*, ppl\_const\_Linear\_Expression\_t *ub*, ppl\_const\_Coefficient\_t *d*) [related]

Assigns to ph the image of ph with respect to the generalized affine transfer relation  $\frac{lb}{d} \leq var' \leq \frac{ub}{d}$ .

#### Parameters

- *ph* The polyhedron that is transformed;
- var The variable bounded by the generalized affine transfer relation;
- *lb* The numerator of the lower bounding affine expression;
- *ub* The numerator of the upper bounding affine expression;
- d The (common) denominator of the lower and upper bounding affine expressions.

#### 7.25.2.24 int ppl\_Polyhedron\_bounded\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, ppl\_const\_Linear\_Expression\_t lb, ppl\_const\_Linear\_Expression\_t ub, ppl\_const\_Coefficient\_t d) [related]

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation  $\frac{lb}{d} \leq var' \leq \frac{ub}{d}$ .

#### **Parameters**

- *ph* The polyhedron that is transformed;
- var The variable bounded by the generalized affine transfer relation;
- *lb* The numerator of the lower bounding affine expression;
- *ub* The numerator of the upper bounding affine expression;
- *d* The (common) denominator of the lower and upper bounding affine expressions.

#### 7.25.2.25 int ppl\_Polyhedron\_generalized\_affine\_image (ppl\_Polyhedron\_t *ph*, ppl\_dimension\_type *var*, enum ppl\_enum\_Constraint\_Type *relsym*, ppl\_const\_Linear\_Expression\_t *le*, ppl\_const\_Coefficient\_t *d*) [related]

Assigns to ph the image of ph with respect to the generalized affine transfer relation  $\operatorname{var}' \bowtie \frac{\operatorname{le}}{\operatorname{d}}$ , where  $\bowtie$  is the relation symbol encoded by relsym.

#### Parameters

- *ph* The polyhedron that is transformed;
- var The left hand side variable of the generalized affine transfer relation;
- *relsym* The relation symbol;
- *le* The numerator of the right hand side affine expression;
- *d* The denominator of the right hand side affine expression.

#### 7.25.2.26 int ppl\_Polyhedron\_generalized\_affine\_preimage (ppl\_Polyhedron\_t ph, ppl\_dimension\_type var, enum ppl\_enum\_Constraint\_Type relsym, ppl\_const\_Linear\_Expression\_t le, ppl\_const\_Coefficient\_t d) [related]

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation  $\operatorname{var}' \bowtie \frac{\mathrm{le}}{\mathrm{d}}$ , where  $\bowtie$  is the relation symbol encoded by relsym.

#### **Parameters**

*ph* The polyhedron that is transformed;

- *var* The left hand side variable of the generalized affine transfer relation; *relsym* The relation symbol;
- *le* The numerator of the right hand side affine expression;
- *d* The denominator of the right hand side affine expression.

#### 7.25.2.27 int ppl\_Polyhedron\_generalized\_affine\_image\_lhs\_rhs (ppl\_Polyhedron\_t *ph*, ppl\_const\_Linear\_Expression\_t *lhs*, enum ppl\_enum\_Constraint\_Type *relsym*, ppl\_const\_Linear\_Expression\_t *rhs*) [related]

Assigns to ph the image of ph with respect to the generalized affine transfer relation  $hs' \bowtie rhs$ , where  $\bowtie$  is the relation symbol encoded by relsym.

#### Parameters

*ph* The polyhedron that is transformed;*lhs* The left hand side affine expression;*relsym* The relation symbol;

*rhs* The right hand side affine expression.

# 7.25.2.28 int ppl\_Polyhedron\_generalized\_affine\_preimage\_lhs\_rhs (ppl\_Polyhedron\_t *ph*, ppl\_const\_Linear\_Expression\_t *lhs*, enum ppl\_enum\_Constraint\_Type *relsym*, ppl\_const\_Linear\_Expression\_t *rhs*) [related]

Assigns to ph the preimage of ph with respect to the generalized affine transfer relation  $lhs' \bowtie rhs$ , where  $\bowtie$  is the relation symbol encoded by relsym.

#### Parameters

*ph* The polyhedron that is transformed;

*lhs* The left hand side affine expression;

*relsym* The relation symbol;

*rhs* The right hand side affine expression.

# 7.25.2.29 int ppl\_Polyhedron\_map\_space\_dimensions (ppl\_Polyhedron\_t ph, ppl\_dimension\_type maps[], size\_t n) [related]

Remaps the dimensions of the vector space according to a *partial function*. This function is specified by means of the maps array, which has n entries.

The partial function is defined on dimension i if i < n and maps[i] != ppl\_not\_a\_dimension; otherwise it is undefined on dimension i. If the function is defined on dimension i, then dimension i is mapped onto dimension maps[i].

The result is undefined if maps does not encode a partial function with the properties described in the *specification of the mapping operator*.

# 7.25.2.30 int ppl\_new\_C\_Polyhedron\_from\_Generator\_System (ppl\_Polyhedron\_t \* pph, ppl\_const\_Generator\_System\_t gs) [related]

Builds a new C polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

# 7.25.2.31 int ppl\_new\_C\_Polyhedron\_recycle\_Generator\_System (ppl\_Polyhedron\_t \* *pph*, ppl\_Generator\_System\_t *gs*) [related]

Builds a new C polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

#### Warning

This function modifies the generator system referenced by gs: upon return, no assumption can be made on its value.

# 7.25.2.32 int ppl\_new\_NNC\_Polyhedron\_from\_Generator\_System (ppl\_Polyhedron\_t \* pph, ppl\_const\_Generator\_System\_t gs) [related]

Builds a new NNC polyhedron from the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

# 7.25.2.33 int ppl\_new\_NNC\_Polyhedron\_recycle\_Generator\_System (ppl\_Polyhedron\_t \* *pph*, ppl\_Generator\_System\_t *gs*) [related]

Builds a new NNC polyhedron recycling the system of generators gs and writes a handle for the newly created polyhedron at address pph.

The new polyhedron will inherit the space dimension of gs.

#### Warning

This function modifies the generator system referenced by gs: upon return, no assumption can be made on its value.

# 7.25.2.34 int ppl\_Polyhedron\_add\_recycled\_generators (ppl\_Polyhedron\_t ph, ppl\_Generator\_System\_t gs) [related]

Adds the system of generators gs to the system of generators of ph.

#### Warning

This function modifies the generator system referenced by gs: upon return, no assumption can be made on its value.

7.25.2.35 int wrap\_assign (ppl\_Polyhedron\_t ph, ppl\_dimension\_type ds[], size\_t n, ppl\_enum\_-Bounded\_Integer\_Type\_Width w, ppl\_enum\_Bounded\_Integer\_Type\_Representation r, ppl\_enum\_Bounded\_Integer\_Type\_Overflow o, const ppl\_const\_Constraint\_System\_t \* pcs, unsigned complexity\_threshold, int wrap\_individually) [related]

Assigns to ph the polyhedron obtained from ph by "wrapping" the vector space defined by the first n space dimensions in ds[].

#### Parameters

- *ph* The polyhedron that is transformed;
- ds[] Specifies the space dimensions to be wrapped.
- *n* The first n space dimensions in the array ds[] will be wrapped.
- w The width of the bounded integer type corresponding to all the dimensions to be wrapped.
- *r* The representation of the bounded integer type corresponding to all the dimensions to be wrapped.
- *o* The overflow behavior of the bounded integer type corresponding to all the dimensions to be wrapped.
- *pcs* Possibly null pointer to a constraint system whose space dimensions are the first n dimensions in ds[]. If \*pcs depends on variables not in vars, the behavior is undefined. When non-null, the constraint system is assumed to represent the conditional or looping construct guard with respect to which wrapping is performed. Since wrapping requires the computation of upper bounds and due to non-distributivity of constraint refinement over upper bounds, passing a constraint system in this way can be more precise than refining the result of the wrapping operation with the constraints in cs.
- *complexity\_threshold* A precision parameter where higher values result in possibly improved precision.
- *wrap\_individually* Non-zero if the dimensions should be wrapped individually (something that results in much greater efficiency to the detriment of precision).

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